

# Generalized expansions of real numbers

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## Abstract

I present here a collection of algorithms that permits the expansion into a finite series or sequence from a real number  $x \in \mathbb{R}$ , the precision used is 64 decimal digits. The collection of mathematical constants was taken from my own collection and theses sources [1]-[6][9][10]. The goal of this experiment is to find a closed form of the sequence generated by the algorithm. Some new results are presented.

- Introduction
- Algorithms
- Results
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## -Introduction

Most of the algorithms will produce a sequence of integers when  $x \in \mathbb{R}$  and can be written as a 2 terms recurrence. If  $x_0$  is the initial value then  $y_n$  will be the terms of the sequence. If  $x_0$  is rational then most of the algorithms will lead to a finite sequence. But with 64 decimal digits enough terms are computed for detecting simple patterns as with some quadratic irrational like  $\sqrt{2}$  or the Golden Ratio. Other numbers like  $e$ , : 2.71828... do have a pattern which is easily recognizable but most real numbers do not. The goal of this computation of sequences from real numbers using different algorithms is to discover or find if there could be any patterns at all with other algorithms.

The natural question that comes to mind is: is there any closed formula or generating function for those sequences? For this I can use Gfun package of Maple or with Mathematica as well to answer the question. Gfun was developed starting in 1991 by me and François Bergeron, see [7]. A known example is  $\sinh(1) = 1.175201193643801456 \dots$  which leads to: 1, 6, 20, 42, 72, 110, 156, 210, 272, 342, ... when expanded into the Engel expansion. That sequence appears to be the coefficients of the series expansion of this rational polynomial:

$$f(x) = \frac{1 + 3x - x^3 + 5x^2}{(1 - x)^3} =$$

$$1 + 6x + 20x^2 + 42x^3 + 72x^4 + 110x^5 + 156x^6 + 210x^7 + \dots$$

So the coefficients are given by the polynomial:  $4n^2 + 2n, n > 1$  by using Montmort formula.

Unfortunately this is a lucky example because for  $\tanh(1) = 0.761\dots$  with the Engel expansion we get: 2, 2, 22, 50, 70, 29091, 49606, 174594, 260086, ... which does not correspond to any known closed formula where the continued fraction expansion of that same numbers is: 0, 1, 3, 5, 7, 9, 11, 13, 15, 17, 19, ....

## -Algorithms

All algorithms begin with  $x_0$  and the sequence is given by the  $y_n$ .

Continued fraction:  $y_n = \left[ \frac{1}{x_n} \right], x_{n+1} = \left\{ \frac{1}{x_{n+1}} \right\}$  will give

$$x = a_0 + \frac{1}{a_1 + \frac{1}{a_2 + \frac{1}{a_3 + \dots}}}$$

Egyptian fraction:  $y_n = \left[ \frac{1}{x_n} \right], x_{n+1} = x_n - \left\{ \frac{1}{y_n} \right\}$  will give

$$x = \frac{1}{a_0} + \frac{1}{a_1} + \frac{1}{a_2} + \frac{1}{a_3} + \frac{1}{a_4} \dots$$

Egyptian product or Engel expansion:  $y_n = \left[ \frac{1}{x_n} \right], x_{n+1} = \{x_n y_n\}$  will give

$$x = \frac{1}{a_0} + \frac{1}{a_0 a_1} + \frac{1}{a_0 a_1 a_2} + \frac{1}{a_0 a_1 a_2 a_3} + \frac{1}{a_0 a_1 a_2 a_3 a_4} \dots$$

Base k (integer) algorithm:  $y_n = [kx_n], x_{n+1} = \{kx_n\}$

Infinite product ( $x > 1$ ):  $y_n = 1 + \left[ \frac{1}{x_n - 1} \right], x_{n+1} = x_n \frac{y_n}{y_{n+1}}$  will give

$$x = \left(1 + \frac{1}{a_0}\right) \cdot \left(1 + \frac{1}{a_1}\right) \cdot \left(1 + \frac{1}{a_2}\right) \cdot \left(1 + \frac{1}{a_3}\right) \cdot \left(1 + \frac{1}{a_4}\right) \dots$$

Infinite product ( $x < 1$ ):  $y_n = 1 + \left[ \frac{1}{|x_n - 1|} \right], x_{n+1} = x_n \frac{y_n}{y_{n-1}}$  will give

$$x = \left(1 - \frac{1}{a_0}\right) \cdot \left(1 - \frac{1}{a_1}\right) \cdot \left(1 - \frac{1}{a_2}\right) \cdot \left(1 - \frac{1}{a_3}\right) \cdot \left(1 - \frac{1}{a_4}\right) \dots$$

Alternated Egyptian product or Pierce expansion:  $y_n = \left[ \frac{1}{x_n} \right], x_{n+1} = 1 - \{x_n y_n\}$  will give

$$x = \frac{1}{a_0} - \frac{1}{a_0 a_1} + \frac{1}{a_0 a_1 a_2} - \frac{1}{a_0 a_1 a_2 a_3} + \frac{1}{a_0 a_1 a_2 a_3 a_4} \dots$$

Factorial base:  $y_n = [n! x(n)], x_{n+1} = x_n - \frac{y_n}{n!}$  will give

$$x = \frac{a_0}{0!} + \frac{a_1}{1!} + \frac{a_2}{2!} + \frac{a_3}{3!} + \frac{a_4}{4!} \dots$$

Prime-Egyptian fraction:  $y_n = 1 + \left[\frac{1}{x_n}\right]$ ,  $y_n = \textit{smallest prime}$ ,  $x_{n+1} = x_n - \frac{1}{y_n}$  will give

$$x = \frac{1}{p_0} + \frac{1}{p_1} + \frac{1}{p_2} + \frac{1}{p_3} + \frac{1}{p_4} \dots$$

Where the  $p_i$  are the smallest possible primes.

## Results

Some expansions are surprising like with the number  $1/24$  in base  $(n^3 e^{2\pi n} - 1)$  gives : [0, 22, 18, 22, 18, 22, 18, 22, 18, 22, 18, 22, 18, 22, 18, 22, 18, 22, 18, 22, 18, ...] which suggests identities like this one.

$$1 = 24 \sum_{n=1}^{\infty} \frac{n^3}{e^{\pi n} - 1} - 264 \sum_{n=1}^{\infty} \frac{n^3}{e^{2\pi n} - 1}$$

These identities were investigated in 2009, 2006 and 1998, a summary is given here:

<http://pictor.math.uqam.ca/~plouffe/inspired3.pdf>

<http://pictor.math.uqam.ca/~plouffe/inspired2.pdf>

<http://pictor.math.uqam.ca/~plouffe/identities.html>

The complete listing of 188 known constants can be found here: <http://pictor.math.uqam.ca/~plouffe/gendev/>

The naming convention used here reflects the fact that these constants are now included in my new database of 2.853 billion constants. One example is given here.

Example with  $\zeta(5)$

**Value x = :**

1.036927755143369926331365486457034168057080919501912811974192678

**Description : Zeta(5)**

Prime-egyptian fraction expansion of  $x$  :

[29,409,114316837,751567899523187,6962015335091299358703666673]

Prime-Engel expansion of  $x$  :

[1,29,17,5,41,11,11,2,17,11,11,5,3,3,3,3,11,5,3,3,3,3,5,3,11,3,3,3,17,7,3,53,29,13,13,11,3,3,37,11,5,2,5,5,11,37,7,7,3,37,19,631,89,179,29,557,127,37,109]

Prime-Pierce expansion of  $x$  :

[1,29,2,11,3,2,2,2,2,2,5,2,3,2,2,11,3,2,2,7,2,3,2,7,2,2,2,11,2,5,2,2,3,2,5,2,2,2,37,2,11,2,2,5,2,2,2,11,2,3,2,2,5,3,2,2,17,2,23,2,3,2,5,2,2,2,5,2,3,2,3,2,3,2,5,2,2,2,5,2,2,7,2,2,2,3,2,11,2,2,2,5,2,5,3,2,2,2,3,2,2,5,2,2,5,2,2,11,3,2,2,2,2,2,2,2,2,2,5,2,2,2,2,2,2,3,2,2,11,2]

Prime-egyptian fraction expansion of  $1/x$  :

[2,3,11,29,179,13241,23590181,9365538893363,11417517410744289132422137]

Prime-Engel expansion of  $1/x$  :

[0,2,2,2,2,3,5,3,3,17,5,2,37,7,11,3,3,5,3,17,5,3,233,379,293,59,11,7,7,11,3,29,79,41,29,7,3,7,11,5,5,3,5,3,5,7,5,2,11,13,37,53,31,17,47,13,23,7,3,17,5,3,11]

Prime-Pierce expansion of  $1/x$  :

[0,2,17,2,3,2,2,2,11,2,2,2,2,2,7,2,2,2,2,2,2,3,2,2,11,2,5,2,2,29,2,5,3,2,2,3,2,3,2,2,2,2,347,2,47,2,11,2,2,5,2,5,2,2,7,2,2,2,2,5,3,2,7,2,11,2,5,2,5,2,2,3,2,7,2,5,2,7,2,2,2,2,2,5,2,2,2,2,11,2,11,2,2,5,2,3,2,5,2,2,1,1,2,2,5,2,2,2,2,2,2,2,2,2,2,2,13,2,11,3,2,2,5,2,2,2,2]

Prime-egyptian fraction expansion of  $1/(1-\text{frac}(x))$  :

[29,263,17047,1553080051,468776062777928639,3306765141393410530618532190714163]

Prime-Engel expansion of  $1/(1-\text{frac}(x))$  :

[1,29,11,5,7,11,7,5,3,13,11,11,5,557,479,83,71,53,11,11,7,11,2,17,5,2,17,179,59,43,59,41,17,5,3,3,5,3,3,31,59,19,19,17,7,61,47,13,7,83,283]

Prime-Pierce expansion of  $1/(1-\text{frac}(x))$  :

[1,29,2,5,2,5,2,3,2,3,2,7,2,5,3,2,2,2,2,5,3,2,2,2,2,2,3,2,5,2,2,3,2,3,2,5,2,2,2,11,2,5,2,2,3,2,5,3,2,2,2,3,2,2,2,2,11,2,3,2,3,2,5,2,2,53,2,11,3,2,2,2,3,2,2,2,11,3,2,2,2,2,2,2,2,5,2,5,3,2,7,2,5,2,2,2,2,2,5,2,2,2,11,2,2,3,2,2,2,2,5,2,53,2,7,2,11,2,2,2,2,2,3,2,2,2,3,2,2,7,2,2,2]

Prime-egyptian fraction expansion of  $1-\text{frac}(x)$  :

[2,3,11,29,233,18119,38735467,132575082674603,876608416457122794673625977]

Prime-Engel expansion of  $1-\text{frac}(x)$  :

[0,2,2,2,2,3,5,11,2,47,127,23,7,3,11,3,7,59,89,79,29,5,13,7,11,11,13,11,13,29,5,5,3,3,19,11,29,19,311,149,67,37,17,11,5,2,17,11,223,23,13,29,7,7,37]

Prime-Pierce expansion of  $1-\text{frac}(x)$  :

[0,2,17,2,2,2,23,2,29,2,5,3,2,5,2,2,2,2,17,2,3,2,2,2,3,2,2,3,2,11,2,2,2,5,2,5,2,2,2,7,2,7,2,2,2,3,2,2,5,2,3,2,2,13,2,5,2,2,2,2,5,3,2,2,2,3,2,5,3,2,2,2,3,2,2,2,2,3,2,3,2,2,2,7,2,3,2,2,2,2,3,2,2,2,37,2,29,2,11,3,2,2,3,2,2,2,2,2,2,2,3,2,7,2,2,2,3,2,3,2,7,2,5,2,2,2,2,2,3,2,3,2,2,2,2,2,2,2,5]

Continued fraction of  $x$  :

[1,27,12,1,1,15,1,5,1,2,19,1,1,32,1,13,1,1,1,3,1,3,2,16,1,12,4,1,5,1,1,1,1,1,2,2,6,1,8,8,6,2,3,2,2,1,30,1,17,116,1,7,1,1,1,1,1,1,2,2,12,1]

Egyptian fraction of  $x$  :

[1,28,825,741721,889339569751,2376584866539240771306852,6154416334529882555528961066901351764864345018895]

Engel expansion of  $x$  :

[1,28,30,52,231,277,523,2278,22749,48854,371305,1447522,1726931,1947729,3657998,6852032]

Engel expansion of  $1/x$  :

[0,2,2,2,2,3,4,7,8,11,52,65,476,648,912,923,1257,1280,2532,25008,65421,69325,143044,1378319,7319579]

Egyptian fraction of  $1/x$  :

[0,2,3,8,166,33433,6993814291,172874227392134456956,994518575001879590886754201389420508674747]

Egyptian fraction of  $1-\text{frac}(x)$  :

[0,2,3,8,212,45599,11664240656,47932007856305467468886,12778435453428804495020574094773636065080706099]

Engel expansion of  $1/(1-\text{frac}(x))$  :

[1,27,29,44,59,63,109,265,519,1010,10268,42272,99420,216617,1558561,11696451,26658373,48867590]

Engel expansion of  $1-\text{frac}(x)$  :

[0,2,2,2,2,3,5,8,11,12,34,91,217,374,1607,7574,12090,15360,50886,100046,1026738,3290030,6805570,7564327]

Egyptian fraction of  $1/(1-\text{frac}(x))$  :

[1,27,766,846085,754028007008,1162069767854581317184367,1720901250519251406854928865230083688568158191814]

Infinite product of  $x$  :

[28,854,1504461,9140342271316,89801131244296097701038584,30301350532971943835822215699316482597179233806905195]

Infinite product of  $1-\text{frac}(x)$  :

[0,28,795,1812251,5081534642389,76162805243343279758282599,26024550802278099021941553504499007822976530719180505]

Infinite product of  $1/(1-\text{frac}(x))$  :

[27,794,1812250,5081534642388,76162805243343279758282598,26024550801465366328614510331474698613599718649143416]

Pierce expansion of  $x$  :

[1,27,338,371,1361,1846,31127,194726,1143811,2634682,7335358,12548979,69987283,1764343077]

Alternated egyptian fraction of  $x$  :

[1,27,9150,129469627,23439855214708089,1973739061445144393762099895522813]



,1,0,1,0,1,0,0,1,0,1,1,0,1,1,0,0,1,0,0,0,0,1,1,0,0,0,1,1,0,1,1,1,1,1,1,  
0,1,1,0,0,1,0,1,1,1,0,1,1,1,1,0,1,0,0,0,1,0,0,1,1,0,1,0,0,1]

Base 10 and prime expansion of  $1/x$  :

[1,13,15,7,5,11,1,6,1,5,0,8,7,2,10,9,10,2,7,5,3,3,4,1,9,1,2,2,7,9,1,1,8,  
8,3,5,2,3,2,3,5,8,4,9,1,2,0,6,5,2,9,4,1,9,1,0,0,1,3]

Base 2 and prime expansion of  $1/(1-\text{frac}(x))$  :

[0,0,0,2,0,1,0,0,1,0,1,1,1,1,1,1,1,0,1,1,1,1,1,1,1,0,0,1,0,0,1,1,1,0,1,  
0,1,1,1,0,1,0,1,1,0,1,0,0,1,0,1,0,0,1,0,1,1,0,0,1,1,0,0,1,0,0,1,0,0,2,0,0,0,0,  
1,1,0,1,0,1,0,0,1,1,0,1,1,1,1,1,0,1,1,0,1,2,0,0,0,0,0,1,0,1,0,0,1,0,1,  
0,1,1,0,1,1,0,0,1,0,1,1,1,1,1,0,0,0,0,1,0,1,1,0,1,0,0,0,1,0,0,1,0,0,0,1,  
0,1,0,1,1,1,1,0,0,1,1,0,0,0,0,1,0,0,0,1,1,1,1,1,1,1,1,1,1,1,1,0,1,1,0,  
0,1,1,0,0,1,0,0,0,0,1,1,0,1,1,0,0,0,1,1,0,1,0,1,1,1,0,1,0,1]

Base 10 and prime expansion of  $1/(1-\text{frac}(x))$  :

[0,1,2,7,1,1,8,7,2,6,0,5,3,4,4,3,5,9,2,7,6,9,0,1,5,8,3,5,5,1,6,8,1,0,4,  
8,9,0,6,9,9,5,9,3,0,7,4,3,3,3,5,1,9,0,8,3,6,0,5]

Base 2 and prime expansion of  $1-\text{frac}(x)$  :

[1,2,2,1,2,0,0,1,0,1,1,0,1,0,1,1,1,0,0,0,0,1,1,0,0,1,0,0,1,0,0,1,0,0,0,  
0,0,1,0,1,1,0,0,0,0,0,1,0,1,1,1,1,1,0,0,0,1,0,1,1,0,1,0,1,1,1,0,0,0,1,  
1,0,0,0,2,0,0,0,0,0,0,1,1,1,1,0,1,0,0,1,0,0,0,0,0,1,1,1,1,0,0,0,1,0,1,  
0,0,1,0,0,1,0,1,1,0,0,1,1,0,1,0,1,1,0,0,0,0,1,1,0,1,1,0,0,0,1,1,0,1,1,  
0,1,1,0,1,1,1,0,1,1,1,1,1,0,1,1,0,0,1,0,1,1,1,0,0,0,0,1,1,1,0,0,1,1,0,  
0,1,0,1,0,0,0,0,1,1,0,0,1,0,1,1,1,1,1,0,1,0,0,1,1,0,1,0,0,1]

Base 10 and prime expansion of  $1-\text{frac}(x)$  :

[1,13,14,12,2,8,4,10,5,1,3,3,3,9,2,11,0,5,10,6,9,9,3,7,0,1,5,9,2,7,6,3,  
1,8,10,3,2,4,2,4,1,9,6,2,2,7,7,8,8,7,1,4,5,5,3,2,5,3,5]

Binary expansion of  $x$  :

[2,0,0,0,1,0,0,1,0,0,1,1,1,0,1,0,0,0,0,0,1,1,0,0,0,1,1,1,0,1,1,0,0,1,0,1,  
0,0,1,1,1,1,1,0,0,1,1,0,0,1,1,0,1,1,0,1,1,0,1,1,1,1,0,1,0,0,0,1,0,0,0,1,  
1,0,0,0,0,0,1,0,0,1,1,1,0,0,0,1,1,1,1,0,1,0,0,0,1,1,0,0,1,1,0,0,1,1,1,  
1,1,1,1,1,0,1,0,0,0,1,1,0,0,0,0,1,0,0,1,1,0,0,0,0,1,0,1,1,1,1,1,1,1,1,  
1,0,1,0,0,0,1,0,0,0,1,0,0,0,0,1,0,0,1,1,1,0,1,1,0,0,1,0,0,1,1,1,1,1,1,  
0,0,1,0,1,1,1,0,1,1,0,1,0,1,0,0,0,1,1,0,1,0,0,1,1,1,1,1,1,1,0,0,1,0,0]

Binary expansion of  $1/x$  :

[1,1,1,1,0,1,1,0,1,1,1,0,0,0,1,0,0,0,0,1,0,1,1,0,1,0,1,1,0,1,1,1,1,1,0,  
1,0,0,0,1,1,1,1,1,0,0,1,0,0,0,1,0,0,0,0,1,0,1,0,1,0,0,1,1,1,0,0,0,0,0,0,  
0,1,1,1,0,0,1,1,0,1,1,1,1,0,1,1,0,0,1,1,0,0,0,1,0,0,0,0,1,1,0,1,1,0,0,  
1,1,1,0,1,0,0,1,0,1,0,1,1,1,1,0,1,1,0,1,0,1,0,0,1,1,1,1,1,1,1,0,0,0,1,1,  
1,0,0,1,1,0,1,1,1,0,1,1,1,0,0,0,1,0,1,1,1,0,0,0,1,1,1,1,1,0,1,0,0,1,1,  
1,1,0,0,1,1,0,1,0,0,0,0,1,0,1,1,0,0,0,0,1,1,1,0,0,0,1,0,1,0,0,0,0,1]

Binary expansion of  $1-\text{frac}(x)$  :

[1,1,1,1,0,1,1,0,1,0,0,0,1,0,1,1,1,1,1,0,0,1,1,1,0,0,0,1,0,0,1,1,0,1,0,  
1,1,0,0,0,0,0,1,1,0,0,1,1,0,0,1,0,0,1,0,0,1,0,0,0,0,1,0,1,1,1,0,1,1,1,0,  
0,1,1,1,1,0,1,1,0,0,0,1,1,1,0,0,0,0,1,0,1,1,1,0,0,1,1,0,0,1,1,0,0,0,  
0,0,0,0,0,0,1,0,1,1,1,0,0,1,1,1,1,0,1,1,0,0,1,1,1,1,0,1,0,0,0,0,0,0,0,  
0,1,0,1,1,1,0,1,1,1,0,1,1,1,1,0,1,1,0,0,0,1,0,0,1,1,0,1,1,0,0,0,0,0,0,  
1,1,0,1,0,0,0,1,0,0,1,0,1,0,1,1,1,0,0,1,0,1,1,0,0,0,0,0,0,0,0,1,1,0,1,1]

Binary expansion of  $1/(1-\text{frac}(x))$  :

[2,0,0,0,1,0,0,1,1,1,0,1,0,0,0,0,1,1,1,0,0,1,0,0,1,0,0,1,0,0,1,0,0,0,0,  
0,0,1,0,0,1,0,0,0,1,1,1,1,0,1,1,1,1,1,0,1,1,1,1,1,0,1,1,1,1,1,1,0,0]

,0,1,1,1,0,0,1,0,1,0,0,1,1,1,1,1,0,1,1,1,1,0,0,0,1,1,0,1,1,0,0,0,1,1,  
0,1,1,1,1,0,1,0,0,1,0,0,1,1,0,0,1,0,1,0,0,0,0,1,0,0,0,1,0,1,0,1,0,1,  
,1,0,0,1,0,1,0,0,1,1,1,0,0,1,0,1,0,0,0,0,0,1,0,1,1,0,1,0,0,1,1,0,0,1,0,  
0,1,0,1,0,0,1,0,0,1,0,0,0,0,1,0,1,1,0,0,1,1,0,0,0,1,1,0,1,1,1,1,0,1,0]

Fibonacci representation of x :

[1,9,12,18,20,23,30,32,35,37,39,41,45,47,49,52,55,57,62,69,73,75,80,90,  
93,96,98,103,107,111,119,125,129,133,141,145,147,153,155,159,164,168,17  
4,181,191,196,199,203,205,208,211,213,215,218,220,223,226,228,231,234,2  
36,238,240,242,244,247,249,254,256,262,267,273,276,281,283,289,292,295,  
301,303,305,307]

Fibonacci representation of 1/x :

[0,3,4,6,13,15,21,24,26,30,33,35,37,39,42,46,53,60,70,74,77,84,86,89,91  
,94,99,101,103,108,110,115,119,123,125,130,133,135,138,144,147,149,151,  
153,161,163,165,170,172,174,179,182,186,188,190,192,194,198,200,203,205  
,216,220,224,226,232,239,243,246,251,254,258,265,272,278,281,283,285,28  
7,289,292,295,297,299,301,303,306]

Lucas representation of x :

[1,7,13,16,20,25,31,34,37,39,41,46,53,58,60,63,71,80,83,85,87,89,94,97,  
100,102,104,106,110,112,115,117,119,121,123,127,134,138,142,147,149,152  
,156,162,164,166,168,176,179,183,189,193,195,197,199,203,206,212,215,21  
9,221,224,227,230,232,235,239,243,250,257,259,261,263,276,279,282,286,2  
88,290,292,294,301,303]

Lucas representation of 1/x :

[0,2,3,4,5,6,7,8,9,10,11,12,13,14,15,16,17,18,19,20,21,22,23,24,25,26,2  
7,28,29,30,31,32,33,34,35,36,37,38,39,40,41,42,43,44,45,46,47,48,49,50,  
51,52,53,54,55,56,57,58,59,60,61,62,63,64,65,66,67,68,69,70,71,72,73,74  
,75,76,77,78,79,80,81,82,83,84,85,86,87,88,89,90,91,92,93,94,95,96,97,9  
8,99,100,101,102,103,104,105,106,107,108,109,110,111,112,113,114,115,11  
6,117,118,119,120,121,122,123,124,125,126,127,128,129,130,131,132,133,1  
34,135,136,137,138,139,140,141,142,143,144,145,146,147,148,149,150,151,  
152,153,154,155,156,157,158,159,160,161,162,163,164,165,166,167,168,169  
,170,171,172,173,174,175,176,177,178,179,180,181,182,183,184,185,186,18  
7,188,189,190,191,192,193,194,195,196,197,198,199,200,201,202,203,204,2  
05,206,207,208,209,210,211,212,213,214,215,216,217,218,219,220,221,222,  
223,224,225,226,227,228,229,230,231,232,233,234,235,236,237,238,239,240  
,241,242,243,244,245,246,247,248,249,250,251,252,253,254,255,256,257,25  
8,259,260,261,262,263,264,265,266,267,268,269,270,271,272,273,274,275,2  
76,277,278,279,280,281,282,283,284,285,286,287,288,289,290,291,292,293,  
294,295,296,297,298,299,300,301,302,303,304,305,306,307]

Fibonacci representation of 1-frac(x) :

[0,3,4,6,13,18,22,28,32,44,54,56,58,60,66,68,70,73,77,80,82,84,88,92,97  
,99,102,104,111,113,120,128,130,132,136,139,141,145,147,150,155,161,163  
,165,167,171,173,179,182,184,186,189,194,198,201,204,210,213,218,221,22  
8,233,235,237,242,245,248,250,254,258,269,276,278,280,284,287,291,299,3  
04,307]

Fibonacci representation of 1/(1-frac(x)) :

[1,9,12,15,19,21,25,28,31,33,35,43,45,48,51,54,56,59,61,63,66,70,72,75,  
77,79,83,87,89,93,95,97,100,105,107,109,114,119,122,128,130,132,135,137  
,139,142,144,148,150,152,158,160,163,165,167,175,177,183,187,190,200,20  
3,208,210,212,214,218,220,227,229,240,242,244,247,251,253,255,259,262,2  
65,271,276,281,286,290,297,300,303,306]



1,1,0,0,0,1,0,1,0,1,0,1,0,1,1,1,0,0,0,1,0,0,0,0,1,1,0,1,1,0,0,0,1,0,0,1  
,1,0,0,0,0,0,0,0,0,1,0,0,1,0,1,0,0,1,0,1,0,1,1,0,1,0,0,1,1,0,0,0,0,0,0,  
0,0,0,0,0,1,0,0,0,0,0,1,0,1,0,0,0,0,0,1,0,1,0,1,0,1,1,0,1,0,0,0,0,0,1,0  
,0,1,0,1,0,1,1,0,1,1,0,1,0,0,0,1,1,0,0,0,0]

Expansion in base  $\exp(2\pi/5)$  of  $x$  :

[3,2,0,3,0,2,2,1,0,0,1,0,1,1,2,0,0,3,1,0,0,0,1,1,2,1,0,2,2,3,0,0,3,1,0,  
1,0,2,2,0,3,1,1,2,1,2,1,0,0,2,1,1,3,0,2,2,2,1,0,0,0,3,0,1,0,1,2,2,3,1,0  
,0,1,2,0,1,0,2,0,1,1,2,1,0,0,1,1,1,1,0,1,2,2,3,1,2,2,3,0,1,1,0,3,1,0,1,  
1,2,3,1,2,0,0,0,2,1,2]

Expansion in base  $\exp(2\pi/5)$  of  $1/x$  :

[3,1,1,0,3,1,2,1,1,2,3,1,1,1,1,0,1,0,1,0,1,1,2,2,3,1,2,0,2,2,0,0,3,0,  
0,2,0,1,1,3,1,0,3,0,0,2,2,0,2,2,0,1,0,2,1,0,2,0,0,1,0,2,0,1,0,3,0,3,0,1  
,2,0,3,1,2,0,3,1,2,2,1,1,3,1,1,0,0,3,0,1,2,2,0,1,1,3,1,1,3,1,2,2,2,3,0,  
0,0,1,2,2,0,2,2,0,2,2]

Expansion in base  $e$  or  $\exp(1)$  of  $x$  :

[2,2,0,1,1,2,0,1,1,0,1,1,2,1,0,1,0,2,0,1,0,1,2,0,0,2,1,1,0,1,2,1,1,0,0,  
2,1,0,2,0,1,2,1,2,0,1,2,1,0,0,0,2,0,2,0,2,1,1,1,1,0,0,2,0,0,0,1,1,0,2,0  
,0,0,1,2,1,2,1,0,2,1,0,2,0,0,1,1,0,0,2,1,1,0,1,0,2,1,0,1,1,1,2,1,2,0,1,  
2,0,2,1,2,0,2,0,0,0,0,2,0,1,1,1,1,0,0,0,2,1,0,2,1,2,1,0,1,2,1,2,0,1,2,0  
,1,0,1,1,2]

Expansion in base  $e$  or  $\exp(1)$  of  $1/x$  :

[2,1,1,2,1,0,0,0,1,0,0,2,0,1,1,0,1,0,0,2,0,1,2,1,0,0,1,0,0,0,0,1,0,1,0,  
1,1,0,0,1,2,0,1,2,0,0,2,0,0,2,1,1,2,0,0,1,1,0,1,2,1,2,0,0,2,0,1,1,0,1,2  
,0,1,2,1,2,0,1,0,0,2,1,1,1,0,1,1,1,0,2,1,0,2,0,1,0,2,1,2,1,0,0,2,0,1,0,  
2,0,2,0,0,2,1,1,0,2,1,0,0,1,1,2,1,2,0,1,1,1,0,2,1,0,2,1,0,2,0,1,0,2,1,1  
,1,2,0,0,2]

Expansion in base  $1+\sqrt{2}$  of  $x$  :

[2,1,0,1,0,1,1,0,0,2,0,1,2,0,2,0,0,1,1,1,0,1,0,0,0,1,0,1,0,0,0,1,1,1,0,  
1,1,2,0,1,1,2,0,1,0,0,1,1,0,1,2,0,1,2,0,0,1,1,0,0,0,2,0,0,1,1,0,0,0,2,0,1,1,0,0,  
1,0,1,2,0,1,0,2,0,0,1,0,1,1,2,0,1,2,0,2,0,2,0,1,1,0,0,0,1,0,1,1,1,2,0,  
1,1,1,2,0,0,1,0,0,0,0,1,1,0,0,2,0,0,0,0,1,1,1,0,0,1,0,0,1,0,0,1,0,1,0,2  
,0,0,0,1,0,0,1,2,0,0,0,0,1,1,0,0,0,0,2,0,1,0,2,0,2]

Expansion in base  $1+\sqrt{2}$  of  $1/x$  :

[2,0,1,2,0,1,0,1,0,0,1,1,1,0,1,1,1,1,0,2,0,2,0,1,0,0,0,2,0,1,1,0,1,0,0,  
1,1,1,0,0,0,0,0,0,1,2,0,1,1,1,0,0,0,1,0,0,0,0,1,2,0,0,0,0,0,2,0,0,0,0,2  
,0,2,0,1,0,2,0,0,1,1,2,0,0,2,0,1,2,0,1,0,0,0,0,0,1,0,0,1,0,0,2,0,1,1,1,  
0,0,2,0,1,0,1,2,0,2,0,0,1,0,1,1,0,0,2,0,1,0,2,0,1,0,2,0,2,0,1,0,0,1,2,0  
,0,0,1,1,0,2,0,1,0,0,0,2,0,0,0,0,0,1,0,1,0,0,0,0,0]

Expansion in base  $\pi$  of  $1-\text{frac}(x)$  :

[3,0,0,0,2,1,1,2,0,2,1,0,0,2,1,1,0,2,0,0,0,2,0,0,2,1,1,0,2,2,0,2,0,2,2,  
1,0,2,2,0,2,2,3,0,0,1,2,0,1,2,1,1,0,2,1,0,2,0,2,0,0,1,1,0,2,1,1,2,2,0,1  
,0,0,2,1,2,2,2,2,1,2,1,1,0,2,1,1,0,0,2,1,2,1,0,1,2,2,3,0,1,0,1,2,1,2,0,  
0,1,1,0,1,2,1,1,1,0,1,2,2,1,2,2,1,1,1,2,0,2]

Expansion in base  $\pi$  of  $1/(1-\text{frac}(x))$  :

[3,0,2,1,2,2,0,0,0,2,2,0,2,2,2,0,2,2,1,0,0,1,1,2,1,1,0,2,2,1,2,0,2,3,0,  
1,0,1,1,1,0,0,3,0,0,1,1,0,1,1,2,1,1,2,2,1,2,2,0,2,1,2,1,1,2,2,2,0,3,0,0  
,0,1,1,1,2,0,1,0,1,3,0,1,0,1,2,0,2,1,0,1,2,0,0,1,2,0,0,1,0,0,0,1,1,2,0,  
2,2,0,1,2,0,1,1,1,3,0,0,1,0,0,0,2,1,2,1,0,2]



Expansion in base  $1+\sqrt{2}$  of  $1/(1-\text{frac}(x))$  :  
[2,1,0,1,0,1,1,2,0,0,0,1,0,1,0,1,0,0,0,1,1,1,0,0,1,1,1,1,2,0,1,0,0,0,1,  
2,0,1,0,1,0,0,0,1,0,0,1,1,2,0,0,0,0,0,2,0,0,2,0,0,2,0,0,2,0,1,0,0,0,1,0  
,2,0,1,1,0,0,0,0,0,0,1,1,1,2,0,1,0,0,0,1,1,0,2,0,1,1,1,0,1,0,0,0,0,0,2,  
0,1,0,1,0,0,0,0,0,1,2,0,0,0,2,0,0,0,1,0,1,1,2,0,1,0,0,2,0,2,0,1,2,0,0,0  
,2,0,1,1,1,2,0,1,0,0,1,1,0,1,1,0,2,0,1,2,0,1,1,2,0]

Expansion in base  $\exp(2\pi n) - 1$  of  $x$  :  
[1,19,395,376,498,477,376,371,246,142,17,260,475,513,30,11,528,467,422,  
408,7,509,405,502]

Expansion in base  $\exp(2\pi n) + 1$  of  $x$  :  
[1,19,433,378,293,488,25,465,386,480,252,396,161,282,431,320,499,514,18  
1,272,237,363,14,514]

Expansion in base  $\exp(\pi n) - 1$  of  $x$  :  
[1,0,19,17,2,6,12,0,14,21,17,13,17,7,4,7,6,4,5,6,9,0,11,13,2,14,17,2,15  
,17,17,0,6,14,16,1,18,18,21,11,1,10,11,2,20,22,18]

Expansion in base  $\exp(\pi n) + 1$  of  $x$  :  
[1,0,19,18,17,4,18,1,17,12,7,2,14,10,21,4,1,4,20,18,4,7,11,5,4,2,9,8,12  
,11,12,11,13,4,4,14,10,8,20,0,19,9,4,20,14,19,13]

Expansion in base  $\pi^n - 1$  of  $x$  :  
[1,0,0,1,0,1,0,0,3,0,0,1,3,0,0,1,2,3,0,1,0,3,0,0,2,2,0,2,2,1,1,0,0,1,0,  
1,2,0,2,3,0,0,1,2,0,1,0,2,1,2,0,0,1,0,0,0,1,1,0,3,0,0,2,1,0,0,3,0,0,2,0  
,1,1,0,0,2,0,0,3,0,0,0,1,0,2,0,2,0,1,2,0,2,2,0,1,1,1,0,0,1,1,1,0,0,0,0,  
1,1,2,0,0,0,0,1,2,1,1,1,0,2,1,3,0,1,0,1,3,0,0]

Expansion in base  $\pi^n + 1$  of  $x$  :  
[1,0,0,1,0,1,2,1,0,0,1,2,0,0,1,0,2,2,2,1,2,1,2,0,0,1,0,1,1,1,1,1,1,2,0,  
1,2,0,0,2,1,2,0,1,0,1,1,0,0,1,1,2,1,2,2,0,0,1,2,1,0,2,0,2,1,2,0,2,1,2,2  
,0,2,1,1,2,2,0,2,3,0,0,0,1,0,3,0,0,0,0,0,1,1,0,0,1,1,2,0,1,2,1,2,2,2,0,  
2,1,0,1,1,2,0,1,2,1,0,1,0,1,1,0,1,0,1,2,1,1,1]

Expansion in base  $2^n - 1$  of  $x$  :  
[1,0,0,0,0,1,0,0,1,0,0,1,1,0,0,0,1,0,0,0,0,0,0,1,0,0,1,1,0,0,1,0,1,1,1,  
1,1,0,1,0,1,1,0,1,0,1,1,0,1,1,0,0,0,0,0,1,0,0,1,0,0,0,1,0,1,1,1,1,1,1,  
,1,1,1,1,0,0,0,1,0,0,0,0,0,0,0,1,0,0,1,1,1,0,1,0,1,0,0,0,0,0,0,0,1,0,1,  
1,0,0,0,0,0,0,1,0,1,1,0,0,0,0,0,1,0,1,0,1,0,1,0,1,1,1,1,1,1,0,0,0,0,0,0  
,0,0,1,1,0,0,0,1,1,0,1,1,1,1,0,1,1,1,0,1,1,1,1,1,0,0,1,1,1,1,1,0,0,1,1,  
1,1,1,0,1,0,1,1,0,0,1,0,1,1,1,1,1,1,0,1,0,1,0,1,0,0,1,1,0,0,0,1,0,1,1,0  
]

Expansion in base  $2^n + 1$  of  $x$  :  
[1,0,0,0,0,1,0,0,1,1,0,1,1,0,0,1,1,0,1,1,0,1,1,0,0,0,1,0,1,0,1,1,0,0,0,  
0,1,1,1,0,0,0,0,0,1,0,1,1,0,0,0,1,0,0,1,1,1,0,0,0,1,1,0,1,1,1,0,1,0,1,0  
,1,0,0,0,0,1,1,0,0,1,0,1,0,0,1,1,1,0,0,0,0,1,1,1,0,0,0,1,1,0,1,1,0,0,1,  
0,0,1,0,1,1,1,0,0,1,0,0,0,0,1,1,1,1,0,0,1,1,0,0,1,0,0,0,0,0,0,0,1,1,1,1,  
,0,1,1,1,1,1,1,1,0,1,1,0,0,0,1,0,0,0,1,0,0,1,1,1,0,1,1,1,1,1,0,1,0,0,  
1,0,1,1,0,0,0,1,1,1,0,1,0,1,1,1,1,1,0,1,1,0,0,0,1,1,0,0,0,1,0,1,1,1,1  
]

Expansion in base  $\exp(n) - 1$  of  $x$  :  
[1,0,0,0,1,2,1,2,1,0,1,2,1,0,2,1,0,0,2,0,2,0,0,0,2,1,1,2,0,1,1,0,0,  
2,0,0,1,1,0,2,1,1,0,1,0,2,1,0,2,1,1,2,1,1,0,2,0,2,0,0,0,0,0,0,2,0,2,0  
,0,2,1,1,1,1,1,1,2,1,1,1,1,1,0,0,1,1,1,1,1,1,1,0,2,0,1,1,0,0,2,0,0,1,



,0,1,1,1,1,1,0,1,1,1,0,0,0,0,1,0,1,0,0,0,1,1,0,1,1,0,0,0,0,1,1,0,1,1,  
1,0,1,0,1,0,1,1,0,1,1,0,1,1,1,1,0,0,1,0,1,1,0,0,0,1,1,1,0,1,1,1,1,1,0  
,0,0,0,0,1,0,1,0,0,0,0,0,0,0,1,1,0,1,0,0,0,1,1,0,1,1,0,0,0,0,0,1,1,1,  
0,1,1,1,0,1,0,0,1,1,1,1,0,0,0,1,0,1,0,0,1,0,1,1,0,0,1,0,1,1,0,1,1,1,1,  
]

Expansion in base  $\exp(n) - 1$  of  $1/x$  :

[0,1,2,1,0,2,1,1,0,0,0,0,2,1,0,0,1,1,0,2,0,2,1,0,2,0,0,0,1,0,1,1,0,1,1,  
2,0,2,1,1,1,1,1,0,0,1,1,0,1,1,2,1,2,0,1,0,0,1,0,2,0,2,0,1,1,0,0,0,0,1,  
,0,1,0,1,0,1,0,1,2,1,1,1,1,1,1,2,0,2,0,2,1,2,1,1,0,2,1,0,2,1,0,2,1,1,2,  
1,1,2,0,0,0,1,0,1,1,2,1,0,0,2,0,2,0,1,1,1,0,2,0,2,0,1,1,2,1,1,1,1,0,1,0  
,0,1,1,1,2,0]

Expansion in base  $\exp(n) + 1$  of  $1/x$  :

[0,3,1,0,2,0,0,2,1,1,2,0,2,1,1,2,0,2,1,0,0,1,2,1,2,0,2,0,1,1,1,2,0,1,0,  
1,1,1,2,1,1,1,2,1,1,0,1,2,1,0,2,0,1,0,1,1,1,1,1,0,1,1,1,1,0,0,2,0,0,1,0  
,0,1,1,1,0,0,1,0,1,0,1,0,2,1,1,2,0,0,2,0,2,1,1,2,1,1,1,1,2,1,1,2,1,0,1,  
2,1,1,0,1,1,1,0,1,1,1,2,0,0,0,2,1,1,2,1,0,1,1,1,2,0,1,0,0,0,1,1,1,1,1,1  
,0,0,1,0,0,0]

Expansion in base  $10^n - 1$  of  $1/x$  :

[0,8,7,4,7,8,7,3,0,6,0,1,5,2,6,0,1,4,6,0,0,9,7,1,6,7,9,7,2,2,9,9,3,9,4,  
3,0,2,7,0,5,2,5,3,3,3,6,2,5,2,2,0,7,9,1,8,0,6,7,7,3,0,3,9,2]

Expansion in base  $10^n + 1$  of  $1/x$  :

[0,10,5,5,7,9,6,5,4,6,7,4,7,3,4,0,9,6,8,3,4,7,2,7,0,7,4,9,0,5,0,3,1,6,4  
,5,6,3,0,3,3,6,1,5,7,2,4,8,5,2,6,0,6,2,7,8,0,3,5,3,2,1,6,2,4]

Expansion in base  $\exp(2\pi*n) - 1$  of  $1-\text{frac}(x)$  :

[0,514,404,298,100,214,459,532,521,384,266,337,93,306,521,3,224,430,532  
,381,109,79,390,434]

Expansion in base  $\exp(2\pi*n) + 1$  of  $1-\text{frac}(x)$  :

[0,516,363,308,257,43,472,37,123,439,469,160,110,100,128,487,475,452,58  
,358,431,156,89,209]

Expansion in base  $\exp(\pi*n) - 1$  of  $1-\text{frac}(x)$  :

[0,21,7,18,12,8,17,10,7,1,15,6,9,5,4,6,20,2,23,2,1,0,13,11,18,17,6,11,2  
,22,17,19,13,1,11,14,14,18,12,10,20,14,16,17,1,20,14]

Expansion in base  $\exp(\pi*n) + 1$  of  $1-\text{frac}(x)$  :

[0,23,5,12,10,7,7,20,6,22,5,8,16,9,10,5,10,14,6,2,21,20,2,21,14,11,17,7  
,7,12,6,16,19,0,22,2,5,20,4,6,14,16,12,19,15,12,1]

Expansion in base  $\pi^n - 1$  of  $1-\text{frac}(x)$  :

[0,2,0,0,2,2,1,2,1,2,0,2,2,2,1,1,0,0,1,1,2,1,1,1,1,0,2,1,0,0,0,1,2,1,1,  
1,0,0,2,1,3,0,0,0,2,0,1,2,1,2,0,2,0,2,1,1,3,0,1,1,0,0,0,0,1,0,0,1,0,2,2  
,0,1,1,2,1,1,2,0,0,1,2,0,2,0,2,2,1,2,0,1,0,2,0,0,0,1,0,2,1,2,0,0,2,0,1,  
2,2,0,1,0,2,1,0,0,1,1,2,3,0,1,0,1,1,2,3,0,0,0]

Expansion in base  $\pi^n + 1$  of  $1-\text{frac}(x)$  :

[0,3,2,1,2,0,3,0,0,0,2,2,1,0,1,2,2,2,2,2,0,0,0,1,1,0,2,2,0,0,0,1,3,0,0,  
2,2,1,2,2,3,0,1,0,1,2,2,2,2,3,0,0,0,2,0,0,2,1,1,1,1,1,1,1,2,1,2,1,1,2,2  
,1,2,1,1,2,1,0,0,1,1,1,0,3,0,1,0,1,1,1,1,0,1,1,2,0,0,1,0,1,1,1,0,1,2,1,  
2,1,0,0,1,0,1,2,0,0,0,0,1,2,1,2,1,2,1,1,0,0,0]

Expansion in base  $2^n - 1$  of  $1-\text{frac}(x)$  :

[0,0,2,2,0,0,0,1,0,1,0,1,1,1,0,0,0,0,1,0,1,1,1,0,0,1,0,1,0,1,1,1,0,1,0,

1,1,0,1,0,1,0,1,0,0,1,1,0,0,0,1,0,1,0,0,0,1,0,0,1,1,1,0,1,1,0,1,0,1,0,0  
,1,1,1,1,0,0,0,0,0,0,0,0,0,0,0,1,1,1,1,0,0,1,0,1,1,1,1,0,0,1,1,1,1,0,0,  
1,0,1,0,1,1,1,0,0,0,1,0,0,0,1,0,0,0,0,0,1,1,1,1,0,0,0,0,1,0,1,0,1,0,0,0  
,1,1,0,0,1,1,0,0,1,0,1,0,0,0,1,1,0,0,0,1,0,0,0,0,0,0,0,0,1,0,1,0,1,0,1,0,  
0,1,0,0,1,1,0,0,1,0,1,1,0,1,0,1,0,1,0,0,1,0,0,1,0,1,1,1,1,0,0,0,1,0,0,1  
]

Expansion in base  $2^n + 1$  of  $1 - \text{frac}(x)$  :  
[0,2,1,0,1,1,0,0,1,1,1,0,1,1,1,1,0,0,1,0,1,1,0,0,1,1,1,0,1,1,0,1,1,0,1,  
0,1,1,0,1,1,0,0,1,1,0,0,0,1,1,0,0,1,0,1,1,0,1,1,1,0,1,0,0,1,1,1,1,1,1,  
,0,1,1,1,1,1,0,1,1,0,1,0,1,0,1,0,0,1,0,1,0,1,1,0,1,0,0,1,1,1,0,1,0,1,1,  
0,1,0,1,0,0,0,1,1,1,1,1,0,1,1,0,1,0,0,0,0,1,0,1,0,1,1,0,1,1,0,0,1,1,1,0  
,1,1,1,1,0,1,1,0,1,0,1,1,0,1,1,0,1,1,0,0,0,0,1,0,0,1,1,1,1,0,0,0,0,1,0,  
0,0,1,0,0,1,0,1,0,0,1,0,0,0,0,0,0,1,1,0,0,0,0,0,0,1,1,0,1,1,1,0,0,0,0,0  
]

Expansion in base  $\exp(n) - 1$  of  $1 - \text{frac}(x)$  :  
[0,1,2,1,0,2,0,2,0,2,0,1,1,0,2,1,1,0,2,1,1,2,0,2,0,2,1,0,1,1,0,0,0,2,1,  
2,0,1,1,0,0,2,0,2,0,2,0,0,1,1,1,1,2,1,0,2,1,1,2,1,0,2,0,2,1,1,1,1,1,1,0  
,2,0,1,1,1,0,0,1,2,0,0,0,2,1,1,1,2,0,2,0,0,2,1,0,1,0,0,0,0,0,0,1,0,1,0,  
0,0,0,0,1,1,2,0,0,0,1,0,1,1,2,0,2,1,2,0,1,0,1,1,2,1,0,1,2,0,1,0,2,1,1,0  
,2,1,1,2,0,1]

Expansion in base  $\exp(n) + 1$  of  $1 - \text{frac}(x)$  :  
[0,3,1,0,2,0,0,1,0,1,0,2,0,2,0,0,2,1,0,0,1,1,0,2,1,0,1,0,0,1,2,0,1,0,2,  
0,1,0,1,1,1,1,2,1,1,2,0,0,1,1,0,1,0,0,1,2,1,0,1,1,1,1,1,0,2,0,2,0,0,0,1  
,2,0,2,0,1,1,1,0,0,0,0,1,1,0,0,2,1,0,1,1,0,2,0,2,0,0,2,1,0,1,0,0,0,0,1,  
0,2,1,0,0,0,0,1,0,1,2,1,0,1,2,1,0,0,1,0,0,1,1,2,0,0,1,0,2,1,0,1,0,0,0,0  
,1,1,1,2,0,2]

Expansion in base  $10^n - 1$  of  $1 - \text{frac}(x)$  :  
[0,8,7,3,4,7,3,2,4,1,5,5,0,6,3,9,6,7,0,5,4,3,5,2,3,7,8,9,0,1,9,8,5,7,4,  
3,4,9,2,1,9,0,8,9,6,0,6,7,8,7,2,5,7,7,4,7,2,8,0,6,7,2,7,1,3]

Expansion in base  $10^n + 1$  of  $1 - \text{frac}(x)$  :  
[0,10,5,4,4,8,0,4,2,2,0,7,0,7,0,0,0,8,3,8,4,1,7,5,3,8,1,8,9,5,9,1,5,5,9  
,3,1,0,5,4,7,3,2,3,0,7,4,2,4,8,7,7,0,0,1,8,0,4,7,3,4,3,6,3,3]

Expansion in base  $\exp(2\pi n) - 1$  of  $1/(1 - \text{frac}(x))$  :  
[1,20,265,126,40,466,434,162,282,277,222,116,524,441,268,258,465,116,49  
8,51,487,412,411,342]

Expansion in base  $\exp(2\pi n) + 1$  of  $1/(1 - \text{frac}(x))$  :  
[1,20,305,127,115,204,3,135,138,470,427,466,520,415,502,441,17,517,62,1  
42,58,392,344,45]

Expansion in base  $\exp(\pi n) - 1$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,20,11,10,15,10,15,21,0,12,7,21,13,7,8,13,21,15,13,9,17,20,5,21,3,1  
7,9,11,9,9,2,7,3,21,9,7,1,10,9,6,17,6,21,10,20,16]

Expansion in base  $\exp(\pi n) + 1$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,20,13,4,9,22,22,1,4,8,18,5,0,15,8,3,8,7,14,10,22,11,9,15,8,8,0,12,  
10,3,1,10,22,7,14,7,13,16,16,4,15,1,4,19,1,2]

Expansion in base  $\pi^n - 1$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,0,1,0,1,1,2,0,1,0,0,1,1,2,0,1,2,1,0,2,2,2,0,2,0,1,1,1,0,2,2,2,0,1,  
2,2,2,2,0,0,3,0,1,1,0,1,1,0,2,3,0,1,0,2,0,0,0,0,2,1,1,1,1,2,2,3,0,0,1,2]

,1,1,2,0,0,1,1,1,1,0,1,1,2,1,2,0,1,1,1,2,2,2,0,0,1,1,1,0,1,1,1,1,2,2,  
1,1,0,1,0,2,1,1,2,2,2,2,1,2,3,0,0,2,1,1,1,0,2]

Expansion in base  $\pi^n + 1$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,1,0,2,0,1,2,1,0,3,0,0,0,3,0,0,0,0,0,1,2,1,1,2,2,0,2,1,1,2,0,1,0,  
1,1,0,0,3,0,0,0,2,1,0,0,0,2,1,2,0,0,2,2,3,0,1,0,2,1,1,3,0,0,1,1,2,1,1,1,  
,1,1,0,0,1,0,1,1,1,2,1,2,0,1,2,0,3,0,0,2,1,1,1,2,1,0,1,0,2,2,0,0,2,2,1,  
1,1,1,1,0,1,2,2,1,0,2,1,2,0,2,3,0,0,0,2,0,1,0]

Expansion in base  $2^n - 1$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,0,1,0,0,1,1,0,0,0,1,1,0,1,1,0,0,1,0,0,1,0,1,0,0,1,1,0,1,1,1,0,  
0,0,1,1,1,1,0,0,1,1,1,0,0,0,1,1,0,0,0,1,0,1,1,0,0,1,0,0,0,1,1,0,0,1,0,1,  
,1,0,0,1,0,0,0,1,1,1,1,0,0,0,0,1,1,0,0,1,1,1,1,0,1,0,1,1,0,1,0,0,1,0,0,  
0,1,1,0,0,1,0,1,0,1,0,0,0,1,1,1,1,1,1,1,0,1,0,1,1,0,1,1,0,1,1,1,0,1,1,1,  
,1,0,0,0,0,0,0,0,1,1,1,1,0,1,0,1,1,1,1,1,0,0,0,0,0,1,0,0,1,0,1,0,0,1,  
1,0,1,1,1,0,0,0,0,1,1,0,1,0,0,0,0,1,0,1,0,1,1,0,1,1,1,0,0,0,1,1,1,0,0,  
]

Expansion in base  $2^n + 1$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,0,1,0,1,0,0,0,0,1,0,0,1,0,1,1,1,0,1,1,0,1,0,0,1,0,1,0,1,0,0,0,  
0,0,1,0,1,0,0,0,0,1,0,0,0,1,0,0,0,1,1,1,0,1,1,1,0,0,1,0,1,1,0,1,0,1,0,0,  
,0,1,1,1,1,0,0,0,1,1,0,1,1,1,1,1,1,0,0,1,0,0,0,0,0,0,1,0,1,1,0,0,0,  
0,1,1,1,1,1,0,0,0,0,1,0,0,1,0,1,1,1,1,0,0,1,0,1,1,1,0,0,0,1,0,1,1,1,1,  
,0,0,0,1,0,0,0,0,0,0,1,1,0,0,0,0,1,1,1,0,0,0,1,1,0,1,0,0,1,0,1,1,0,0,  
1,0,0,0,1,0,1,1,0,0,1,0,1,0,1,1,0,0,0,0,1,1,1,1,0,0,1,1,0,0,0,1,0,0,1,1,  
]

Expansion in base  $\exp(n) - 1$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,2,0,0,1,0,0,2,1,1,1,0,1,0,1,0,1,1,1,2,1,1,2,0,2,0,1,2,1,0,1,0,  
0,0,2,1,0,1,1,0,0,2,1,0,1,0,2,1,2,0,2,0,0,0,2,1,0,0,0,0,1,0,2,1,1,0,0,1,  
,0,0,0,2,0,0,2,1,2,0,2,0,2,0,1,2,0,0,1,2,0,2,0,0,1,0,1,0,2,0,2,0,0,1,2,  
0,1,0,0,0,1,0,1,2,0,1,0,0,1,1,0,0,1,0,1,1,0,1,0,2,1,1,1,1,2,1,1,0,2,1,1,  
,2,0,0,1,1,2]

Expansion in base  $\exp(n) + 1$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,2,0,0,2,1,1,1,2,1,2,1,0,1,0,1,1,2,0,1,1,0,1,2,1,0,2,0,1,2,0,2,  
1,0,1,0,1,1,1,0,1,2,1,1,0,1,1,2,1,0,2,0,2,0,1,0,0,1,1,0,0,1,0,1,0,1,0,2,  
,0,2,1,0,0,1,0,2,1,1,0,1,0,0,2,0,2,1,0,0,0,1,1,2,1,1,2,0,0,1,2,0,0,2,1,  
0,2,1,0,2,1,1,1,1,1,0,1,0,0,2,0,0,0,1,2,1,1,0,0,0,1,1,1,1,2,1,0,0,2,0,1,  
,0,1,2,0,0]

Expansion in base  $10^n - 1$  of  $1/(1-\text{frac}(x))$  :

[1,0,3,8,0,3,2,6,6,3,3,6,8,3,2,8,6,2,5,5,4,6,4,0,5,3,5,4,2,6,3,8,5,0,7,  
6,6,4,5,1,6,8,2,6,4,6,5,2,4,4,7,0,8,7,3,9,0,0,7,0,6,8,0,8,9]

Expansion in base  $10^n + 1$  of  $1/(1-\text{frac}(x))$  :

[1,0,3,8,6,4,8,7,8,4,0,9,4,4,6,0,2,4,2,6,4,6,9,5,3,3,2,5,3,9,2,1,8,8,3,  
9,0,5,6,3,5,1,3,9,3,3,1,0,0,5,3,0,3,0,2,8,6,1,2,5,9,9,0,1,6]

Expansion in base  $(n \cdot \exp(2 \cdot \pi \cdot n) - 1)$  of  $x$  :

[1,19,791,327,396,22,435,461,491,28,87,429,34,263,550,146,290,536,57,16  
1,286,172,441,469]

Expansion in base  $(n \cdot \exp(2 \cdot \pi \cdot n) + 1)$  of  $x$  :

[1,19,867,332,294,61,620,402,117,225,532,71,122,44,495,413,16,133,236,1  
64,259,254,436,156]





Expansion in base  $(n \cdot \exp(n) + 1)$  of  $1/x$  :

[0,3,2,2,1,1,2,0,1,3,0,0,1,0,0,0,1,2,1,0,0,1,2,0,0,0,0,1,2,1,1,0,0,1,0,  
2,0,0,0,1,2,0,1,1,1,2,1,1,1,1,1,0,2,0,2,2,0,0,0,0,0,2,1,2,0,1,2,1,1,0,2  
,1,1,0,1,1,1,0,2,0,1,0,0,2,0,2,1,0,1,2,1,0,2,0,1,0,2,0,0,0,1,1,0,0,2,0,  
2,0,1,0,0,1,2,0,2,0,1,0,1,1,1,2,0,1,2,1,0,2,1,1,2,0,0,0,0,0,2,1,0,1,2,1  
,0,1,0,2,0,2]

Expansion in base  $(n \cdot 10^n - 1)$  of  $1/x$  :

[0,8,14,14,4,10,0,2,3,2,8,4,4,0,8,4,9,4,1,5,2,1,7,5,5,6,3,2,6,5,7,10,2,  
9,0,3,0,5,3,3,5,0,9,3,5,5,6,4,4,9,6,9,3,7,0,8,3,6,7,5,6,3,8,0,8]

Expansion in base  $(n \cdot 10^n + 1)$  of  $1/x$  :

[0,10,11,2,7,0,0,0,2,1,1,5,4,7,6,6,2,5,10,2,1,0,0,9,9,10,0,9,6,5,3,7,3,  
3,7,5,3,9,4,5,1,9,9,5,2,2,3,0,6,2,9,6,7,1,2,4,0,6,8,1,0,0,3,1,8]

Expansion in base  $(n \cdot \exp(2 \cdot \pi \cdot n) - 1)$  of  $1 - \text{frac}(x)$  :

[0,514,809,91,230,32,190,369,382,288,173,245,460,554,386,266,218,433,31  
,307,356,435,142,147]

Expansion in base  $(n \cdot \exp(2 \cdot \pi \cdot n) + 1)$  of  $1 - \text{frac}(x)$  :

[0,516,727,122,146,518,379,235,450,389,111,374,4,7,236,24,452,347,74,25  
0,345,381,167,487]

Expansion in base  $(n \cdot \exp(\pi \cdot n) - 1)$  of  $1 - \text{frac}(x)$  :

[0,21,15,20,25,18,26,20,6,4,0,5,23,10,17,21,21,5,9,15,15,20,23,0,22,16,  
22,4,13,10,17,6,1,13,9,17,4,3,8,23,16,15,11,20,14,3,17]

Expansion in base  $(n \cdot \exp(\pi \cdot n) + 1)$  of  $1 - \text{frac}(x)$  :

[0,23,11,2,21,6,27,16,16,20,22,2,25,0,17,16,24,12,21,1,9,22,4,13,0,11,1  
0,18,14,9,20,4,19,8,17,9,8,7,14,3,1,12,3,18,19,8,20]

Expansion in base  $(n \cdot \pi^n - 1)$  of  $1 - \text{frac}(x)$  :

[0,2,0,2,2,2,2,2,2,1,0,2,2,1,2,1,2,1,2,2,1,1,2,1,1,0,0,1,2,2,0,0,1,1,2,  
0,0,2,1,0,1,2,1,0,1,3,0,0,0,0,2,1,1,2,0,3,0,0,1,1,1,1,2,0,3,0,0,2,1,1,1  
,0,2,1,2,1,1,0,1,1,0,2,0,1,2,0,1,0,0,1,0,2,1,2,1,2,1,2,1,2,2,0,0,0,2,3,  
0,0,2,1,1,2,0,2,1,2,1,2,0,2,2,2,1,1,1,1,0,2,0]

Expansion in base  $(n \cdot \pi^n + 1)$  of  $1 - \text{frac}(x)$  :

[0,3,5,0,3,1,2,2,0,0,0,1,1,2,0,1,0,1,0,2,2,0,2,2,0,2,0,2,1,0,0,0,0,2,3,  
0,2,1,0,0,0,2,0,2,3,0,1,1,0,2,2,0,2,1,2,0,0,0,1,0,0,1,2,0,1,2,2,2,2,1,2  
,2,3,0,1,1,0,0,2,0,2,0,2,2,2,1,1,1,2,2,3,0,1,0,1,2,0,1,1,0,1,1,0,1,2,0,  
1,2,0,3,0,0,2,1,2,0,0,2,2,0,0,1,2,0,2,1,2,0,2]

Expansion in base  $(n \cdot 2^n - 1)$  of  $1 - \text{frac}(x)$  :

[0,0,5,2,2,0,0,1,0,0,0,0,2,0,0,0,2,0,0,0,0,0,1,1,0,0,0,0,0,1,1,1,1,0,1,  
1,1,0,1,0,0,1,1,0,0,1,0,0,0,1,0,0,1,0,1,0,1,1,1,0,0,0,1,0,1,0,0,0,1,1,1  
,1,1,0,1,1,0,0,1,1,1,0,1,0,0,0,0,0,2,0,0,0,0,0,1,0,1,1,0,1,0,0,0,1,1,1,  
0,0,1,0,1,0,1,0,1,0,0,1,0,0,0,0,1,0,1,1,0,1,0,0,0,0,0,1,1,0,0,1,0,1,0,0  
,0,0,1,1,0,1,1,0,0,0,0,0,0,1,1,0,0,0,0,1,0,1,0,0,0,1,1,1,0,0,0,0,1,1,  
0,1,0,0,0,0,1,2,0,0,0,0,0,0,0,0,1,1,0,1,0,1,1,0,1,1,1,1,0,0,1,0,1,0,0,0  
]

Expansion in base  $(n \cdot 2^n + 1)$  of  $1 - \text{frac}(x)$  :

[0,2,2,2,1,1,0,1,0,2,0,0,1,0,0,2,0,0,0,0,0,0,0,1,0,0,0,0,0,1,1,1,0,1,0,  
1,0,1,1,2,0,0,0,0,1,1,1,0,0,0,0,1,0,0,1,1,1,0,0,0,1,1,1,0,0,1,1,1,0,1,1  
,1,0,0,1,0,1,0,0,1,1,0,0,1,1,0,0,1,0,1,0,1,0,0,0,1,1,0,1,1,0,1,0,0,0,0,  
1,1,0,1,1,1,0,0,1,0,1,1,1,0,1,0,0,0,0,0,1,1,0,0,0,0,0,0,1,0,1,1,1,1,1,0  
,1,0,0,1,0,0,1,1,0,0,0,0,0,0,0,1,1,1,0,1,0,0,0,1,1,0,1,2,0,0,0,0,0,0,1,

0,1,1,0,0,1,0,1,1,0,1,0,0,0,1,1,0,1,0,1,1,0,0,1,0,0,0,0,0,0,0,0,0,1,0,0,1  
]

Expansion in base  $(n \cdot \exp(n) - 1)$  of  $1 - \text{frac}(x)$  :

[0,1,4,3,3,1,0,2,1,0,2,1,2,2,1,2,1,1,2,1,1,1,1,1,1,0,2,1,1,2,1,2,0,1,2,  
0,0,0,0,0,2,1,0,0,2,1,2,1,0,1,1,0,1,0,0,1,1,1,0,1,1,2,1,2,1,1,2,0,0,2,0  
,0,2,0,2,0,1,0,1,2,1,1,1,1,2,0,1,2,0,0,0,1,1,0,0,0,1,2,0,0,0,2,0,1,0,2,  
1,2,1,1,2,0,1,0,2,1,2,0,1,2,1,0,2,0,1,0,2,1,1,1,2,1,2,1,0,0,1,1,2,0,2,0  
,2,1,1,0,1,0]

Expansion in base  $(n \cdot \exp(n) + 1)$  of  $1 - \text{frac}(x)$  :

[0,3,2,2,1,0,2,0,2,1,2,0,0,2,1,0,2,0,1,0,0,1,2,0,2,1,0,0,2,0,0,0,0,2,1,  
1,0,2,1,2,0,1,2,0,1,1,2,1,0,2,0,2,1,1,2,2,0,0,2,1,0,2,0,0,0,1,1,1,1,0,1  
,0,0,1,2,1,1,2,1,2,0,0,0,2,1,1,0,1,2,0,2,1,1,1,2,0,0,0,1,1,0,1,1,2,1,1,  
2,1,1,2,1,1,2,1,1,0,1,0,1,2,0,0,0,0,0,2,0,0,0,2,1,2,0,0,0,0,0,0,0,0,2  
,0,0,0,1,0,1]

Expansion in base  $(n \cdot 10^n - 1)$  of  $1 - \text{frac}(x)$  :

[0,8,14,10,5,7,3,7,2,1,0,4,9,9,7,8,2,9,7,6,4,8,10,1,8,0,9,0,7,1,10,2,3,  
9,2,7,1,7,0,9,2,2,3,3,6,5,9,2,4,0,4,2,9,3,2,4,2,3,1,3,3,7,0,4,2]

Expansion in base  $(n \cdot 10^n + 1)$  of  $1 - \text{frac}(x)$  :

[0,10,10,13,5,11,2,4,2,6,1,8,7,5,3,5,0,9,5,0,6,1,4,2,5,1,4,5,10,1,10,2,  
6,1,1,8,4,0,0,8,5,5,4,1,8,3,3,6,3,7,1,10,1,5,1,4,6,5,1,6,1,7,10,1,0]

Expansion in base  $(n \cdot \exp(2 \cdot \text{Pi} \cdot n) - 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,20,530,378,163,325,617,521,451,363,86,72,340,343,498,18,44,441,175,2  
94,215,414,65,522]

Expansion in base  $(n \cdot \exp(2 \cdot \text{Pi} \cdot n) + 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,20,610,381,461,350,427,522,508,177,128,261,97,92,114,278,531,71,106,  
329,311,326,1,325]

Expansion in base  $(n \cdot \exp(\text{Pi} \cdot n) - 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,0,40,34,11,23,16,20,25,16,16,1,19,0,17,2,10,13,5,22,11,2,19,11,10,22  
,20,10,5,9,15,5,1,15,13,11,16,16,22,17,1,1,2,15,4,1,12]

Expansion in base  $(n \cdot \exp(\text{Pi} \cdot n) + 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,0,41,4,28,15,26,23,5,11,4,24,21,6,15,11,21,16,16,16,16,4,11,4,4,16,1  
1,5,19,4,6,10,19,19,1,1,8,2,3,0,5,23,5,23,6,0,16]

Expansion in base  $(n \cdot \text{Pi}^n - 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,0,0,3,1,3,2,2,1,0,2,0,1,1,0,0,0,0,1,2,2,0,1,0,1,0,0,1,0,2,3,0,2,1,1,  
3,0,0,3,0,0,2,1,3,0,1,0,0,1,2,1,2,2,2,2,1,1,1,0,2,1,0,0,1,2,1,2,1,2,1,2  
,0,1,1,0,1,2,1,0,0,1,0,0,0,2,1,1,2,1,0,2,2,0,1,2,3,0,0,2,0,0,0,2,1,0,3,  
0,1,1,2,1,0,2,0,1,2,2,2,2,2,0,0,3,0,1,0,0,1,0]

Expansion in base  $(n \cdot \text{Pi}^n + 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,0,0,3,2,3,0,1,1,1,0,1,2,2,0,0,2,0,0,0,3,0,1,0,1,3,0,1,1,1,0,1,2,2,2,  
2,1,1,1,2,0,1,2,1,2,2,1,2,0,2,1,1,0,1,1,1,1,3,0,1,0,1,0,1,1,2,3,0,0,1,1  
,2,1,3,0,1,2,0,3,0,0,0,0,3,0,0,0,2,0,2,0,2,2,0,2,0,2,1,2,2,1,2,2,2,2,1,  
3,0,1,2,0,2,2,1,1,2,2,0,1,1,1,2,2,0,2,2,0,0,2]

Expansion in base  $(n \cdot 2^n - 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,0,0,0,2,0,1,2,0,0,1,0,0,1,1,1,1,1,0,2,0,0,0,1,0,1,0,0,1,1,0,1,1,0,0,  
0,0,0,1,0,1,1,0,1,0,2,0,0,0,0,0,2,0,0,0,0,0,1,1,0,0,0,0,1,0,1,0,0,0,1,0  
,1,0,0,0,1,1,0,0,0,1,1,1,1,0,0,1,0,0,0,0,1,1,1,0,0,0,0,1,0,1,1,0,0,1,1,  
0,1,1,1,0,1,1,0,1,0,1,1,1,0,0,1,0,0,1,1,1,0,0,0,1,1,0,0,0,1,1,1,1,1,1,0

,1,1,0,0,1,0,0,0,1,1,0,0,0,0,1,0,0,0,1,0,0,0,1,1,0,0,1,0,1,1,1,1,1,1,0,  
0,1,1,1,0,0,0,0,1,0,1,0,0,0,1,0,0,1,1,0,0,1,0,1,1,1,1,0,0,1,0,1,0,1,0,0  
]

Expansion in base  $(n^2^n + 1)$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,1,0,0,0,1,0,0,2,0,0,0,0,2,0,0,0,0,1,0,0,1,0,1,0,1,0,0,1,1,1,1,1,  
1,1,1,1,0,1,0,0,1,1,0,1,1,0,0,1,0,1,0,1,0,0,0,1,0,1,1,0,1,0,1,1,1,1,1,1,  
,1,0,1,0,0,1,1,1,0,1,0,0,2,0,0,0,0,0,1,0,1,1,0,1,0,1,0,1,0,1,1,1,1,1,1,  
1,0,0,0,1,1,0,1,0,1,1,1,1,0,1,1,0,1,1,1,0,1,1,0,0,0,0,1,0,0,1,0,1,0,0,1,  
,0,0,1,0,1,1,1,1,0,1,1,0,1,1,0,1,0,1,1,1,1,0,1,0,1,1,1,1,0,0,1,0,0,0,1,  
1,0,1,1,0,0,1,1,1,1,1,1,1,1,0,0,0,0,0,0,0,0,1,0,1,0,1,1,0,0,1,1,0,1,1,1,1,  
]

Expansion in base  $(n^{\exp(n)} - 1)$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,2,0,2,1,2,0,1,2,1,1,0,0,1,0,1,0,2,1,1,1,0,2,0,2,0,2,0,0,2,0,2,1,  
1,0,1,0,0,2,0,1,2,1,0,0,1,2,1,1,1,1,1,1,2,1,0,2,1,2,0,1,1,0,2,0,2,1,0,0,1,  
,1,0,1,0,1,1,1,1,0,2,0,1,0,1,1,0,1,2,1,1,1,0,1,1,2,1,0,0,1,0,2,0,0,2,1,  
0,0,2,1,1,2,1,0,1,0,1,0,2,1,0,1,1,0,2,1,1,1,0,1,1,1,1,0,1,0,0,1,1,2,0,1,  
,1,2,0,0,1,0]

Expansion in base  $(n^{\exp(n)} + 1)$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,2,1,1,2,0,1,1,2,1,1,2,0,1,2,0,1,1,2,2,0,1,1,0,0,1,0,0,1,0,1,1,0,  
1,2,0,1,2,0,2,0,1,0,2,0,2,1,2,1,2,1,0,1,1,1,2,0,2,0,0,2,1,2,1,0,1,1,1,1,  
,1,0,2,0,0,1,0,1,1,1,0,2,0,1,1,2,1,1,2,1,2,0,1,2,0,1,2,1,0,0,0,2,1,1,1,  
1,1,0,0,1,0,0,2,1,0,1,0,2,0,0,2,1,1,0,0,2,0,2,1,0,1,1,1,0,2,1,2,0,0,2,0,  
,1,2,0,1,0,2]

Expansion in base  $(n^{10^n} - 1)$  of  $1/(1-\text{frac}(x))$  :

[1,0,7,8,12,10,4,9,4,1,7,2,6,2,5,7,3,8,4,10,3,6,5,2,7,2,7,2,6,6,6,7,6,4,  
,7,2,2,5,0,7,9,9,7,1,10,0,2,3,8,5,9,5,10,0,1,1,3,2,7,0,9,2,6,9,6]

Expansion in base  $(n^{10^n} + 1)$  of  $1/(1-\text{frac}(x))$  :

[1,0,7,11,1,1,1,4,9,3,9,9,9,3,3,5,4,7,9,7,4,7,9,8,4,4,1,2,4,3,0,1,9,2,1,  
,4,1,8,8,6,3,3,7,4,5,4,3,8,5,9,0,7,6,1,7,9,3,2,4,7,4,9,2,1,7]

Expansion in base  $(n^{2^{\exp(2\pi^n)}} - 1)$  of  $x$  :

[1,19,1582,982,632,125,614,714,88,466,43,277,121,290,332,51,102,266,17,  
438,98,361,78,369]

Expansion in base  $(n^{2^{\exp(2\pi^n)}} + 1)$  of  $x$  :

[1,19,1734,997,224,322,190,128,386,288,131,178,308,353,34,240,226,517,1  
48,222,119,459,465,465]

Expansion in base  $(n^{2^{\exp(\pi^n)}} - 1)$  of  $x$  :

[1,0,78,49,23,13,2,29,24,16,6,11,2,25,4,21,19,9,6,21,17,22,6,11,12,0,9,  
11,6,6,19,13,16,4,15,12,20,14,1,2,8,6,19,12,2,18,18]

Expansion in base  $(n^{2^{\exp(\pi^n)}} + 1)$  of  $x$  :

[1,0,79,12,31,26,20,17,7,4,20,26,13,19,15,11,15,22,18,17,11,25,7,8,20,1  
1,22,6,14,24,1,4,0,20,17,19,20,22,14,0,7,18,18,17,11,6,19]

Expansion in base  $(n^{2^{\pi^n}} - 1)$  of  $x$  :

[1,0,1,2,2,0,1,1,2,0,1,3,2,3,0,1,3,0,0,3,1,0,2,0,1,1,1,3,0,1,2,1,1,0,3,  
0,3,0,1,2,2,1,2,0,0,2,0,1,2,3,0,0,0,1,2,0,1,0,0,1,1,1,0,2,1,2,1,2,0,2,1,  
,1,0,1,0,0,0,2,1,2,1,2,0,1,0,2,0,1,2,0,2,2,0,0,1,1,1,1,2,2,1,1,3,0,0,  
0,1,0,3,0,1,2,0,2,1,2,0,0,1,3,0,1,2,0,0,1,0,1]

Expansion in base  $(n^2 \cdot \pi^n + 1)$  of  $x$  :

[1,0,1,4,0,0,1,1,3,2,2,2,2,1,0,0,0,0,1,1,2,0,2,1,3,1,1,0,1,2,2,0,2,2,1,  
1,0,3,0,0,3,0,2,0,1,3,0,2,2,1,2,1,0,1,1,1,1,3,0,1,2,3,0,1,2,1,2,2,2,2,  
,1,0,1,1,2,2,1,2,2,0,0,2,1,2,0,2,0,2,0,3,0,0,2,0,1,0,1,0,3,0,0,2,1,3,0,  
1,2,1,1,2,2,2,1,0,1,2,0,0,0,0,1,2,2,1,0,2,2,0]

Expansion in base  $(n^2 \cdot 2^n - 1)$  of  $x$  :

[1,0,0,2,1,0,2,0,2,0,1,0,0,1,0,1,0,1,1,0,0,1,2,0,0,1,0,0,0,0,1,1,1,0,1,  
2,0,0,0,0,0,1,1,0,1,0,0,2,0,0,0,0,1,0,1,0,0,1,1,1,1,1,1,1,0,0,0,0,0,1,1  
,0,1,0,0,0,0,1,0,1,1,1,0,0,1,1,1,0,1,2,0,0,0,0,1,0,1,1,0,1,1,1,0,1,1,1,  
0,0,1,1,0,0,2,0,0,0,0,0,1,1,0,1,1,1,0,1,1,0,0,1,0,1,1,1,0,0,1,0,1,1,0,1  
,1,1,0,1,0,0,0,1,0,0,0,1,0,1,1,0,0,1,1,0,0,0,0,1,1,1,1,0,1,0,1,2,0,0,0,  
0,0,1,0,0,1,1,1,0,1,1,0,0,1,0,1,1,0,1,1,1,1,0,0,0,1,1,0,1,1,0,0,1,0,0,0  
]

Expansion in base  $(n^2 \cdot 2^n + 1)$  of  $x$  :

[1,0,0,2,3,0,2,2,0,1,1,0,1,0,1,0,0,1,2,0,0,0,1,1,0,1,0,1,0,1,1,1,2,0,0,  
0,0,0,0,1,0,0,0,1,1,1,1,0,0,0,1,1,1,0,0,0,1,1,1,1,1,1,0,1,0,1,1,0,0,1,0  
,0,1,1,1,1,0,1,0,0,1,0,1,1,1,1,1,1,0,1,0,1,0,0,1,1,0,1,2,0,0,0,0,0,1,  
0,1,0,1,0,2,0,0,0,0,0,1,0,1,1,0,0,1,0,0,0,1,1,1,0,0,1,0,2,0,0,0,0,0,1,1  
,0,1,1,0,1,0,0,0,0,0,1,1,1,0,1,0,1,1,0,1,0,0,0,1,2,0,0,0,0,0,1,0,1,0,0,  
0,0,1,1,1,0,1,1,0,1,2,0,0,0,0,0,1,0,0,1,0,1,0,0,0,1,1,1,1,0,1,1,1,1,1,0  
]

Expansion in base  $(n^2 \cdot \exp(n) - 1)$  of  $x$  :

[1,0,0,6,1,3,0,0,3,0,3,0,1,2,1,1,0,0,0,2,1,0,1,1,2,0,2,2,1,0,2,2,1,1,1,  
2,1,1,1,0,2,0,1,1,2,1,1,2,1,2,0,0,1,0,2,0,0,0,1,0,1,0,2,1,0,1,1,0,1,0,1  
,1,0,0,0,2,1,1,0,0,2,0,1,0,0,1,1,0,0,1,2,0,0,0,2,0,2,0,0,2,0,2,0,0,1,1,  
0,1,1,0,2,0,1,0,1,2,1,0,0,0,1,0,1,2,1,0,1,0,2,1,1,1,0,0,0,1,2,1,1,1,0,1  
,0,1,1,1,1,0]

Expansion in base  $(n^2 \cdot \exp(n) + 1)$  of  $x$  :

[1,0,1,1,1,2,2,3,0,3,0,1,1,1,1,1,1,0,2,0,0,1,2,2,2,0,0,0,2,1,2,1,1,1,2,  
1,0,0,0,1,1,1,1,2,0,2,1,0,1,0,0,0,0,2,1,0,2,1,0,0,1,0,1,2,1,0,2,0,1,0,1  
,1,1,1,0,0,2,1,1,1,1,1,2,0,2,1,0,0,0,2,1,0,2,0,0,0,1,1,1,1,2,0,0,0,0,1,  
1,1,0,1,2,0,0,1,2,0,1,0,0,0,1,0,0,1,1,0,2,0,0,0,1,2,0,0,0,1,1,0,1,0,2,1  
,0,2,1,0,0,2]

Expansion in base  $(n^2 \cdot 10^n - 1)$  of  $x$  :

[1,0,14,14,2,11,7,5,7,6,10,11,4,4,9,4,3,1,1,8,5,10,6,8,7,3,3,9,6,4,4,0,  
7,9,7,3,9,5,1,3,6,9,0,0,3,9,7,9,9,5,10,3,4,3,7,1,9,7,1,2,4,3,4,1,10]

Expansion in base  $(n^2 \cdot 10^n + 1)$  of  $x$  :

[1,0,14,20,8,10,10,7,3,6,10,3,6,10,5,0,8,5,6,4,4,8,4,8,9,4,1,5,9,2,0,9,  
8,0,0,5,2,5,6,1,9,8,2,5,6,6,2,4,6,7,2,4,1,2,5,2,7,5,4,9,6,5,4,2,6]

Expansion in base  $(n^2 \cdot \exp(2 \cdot \pi \cdot n) - 1)$  of  $1/x$  :

[0,515,980,815,693,349,388,507,141,429,496,512,315,34,246,607,329,245,3  
24,580,254,41,191,38]

Expansion in base  $(n^2 \cdot \exp(2 \cdot \pi \cdot n) + 1)$  of  $1/x$  :

[0,517,824,903,80,214,302,142,235,17,57,284,13,347,430,190,219,197,213,  
166,401,77,59,474]

Expansion in base  $(n^2 \cdot \exp(\pi \cdot n) - 1)$  of  $1/x$  :

[0,21,34,0,20,34,14,4,0,26,26,1,17,6,4,12,10,24,3,21,12,22,16,19,4,1,7,  
10,5,9,2,13,4,12,9,21,20,24,8,21,15,21,20,23,4,18,21]

Expansion in base  $(n^2 \cdot \exp(\pi \cdot n) + 1)$  of  $1/x$  :  
[0,23,24,50,32,26,18,24,25,28,19,10,25,16,23,11,25,25,17,9,20,13,13,18,  
24,5,9,9,4,1,9,4,12,23,19,13,17,18,10,17,7,12,20,22,20,10,3]

Expansion in base  $(n^2 \cdot \pi^n - 1)$  of  $1/x$  :  
[0,2,1,0,3,2,3,3,1,2,1,1,0,1,1,1,2,0,2,1,1,0,2,3,0,0,0,3,1,0,3,0,1,0,1,  
1,2,1,1,2,2,0,1,0,0,0,3,0,0,0,2,0,0,1,2,1,2,2,2,0,3,0,1,2,1,2,1,2,0,2,1,  
,2,0,0,2,1,2,0,2,2,2,0,3,0,1,1,1,2,1,3,0,1,1,0,3,0,0,2,2,0,3,0,0,1,1,2,  
2,0,0,0,0,1,1,2,2,1,1,2,1,2,3,0,1,2,1,1,0,2,2]

Expansion in base  $(n^2 \cdot \pi^n + 1)$  of  $1/x$  :  
[0,3,10,2,4,4,0,3,2,2,1,0,2,1,2,2,0,2,1,2,1,0,1,2,0,2,2,1,2,2,0,1,0,1,1,  
,1,1,0,1,2,2,3,0,1,0,2,0,2,0,1,2,1,1,2,0,0,1,1,2,2,2,1,2,0,0,0,1,2,0,3,  
0,0,0,2,1,3,0,0,3,0,2,0,0,0,1,2,2,1,0,0,2,0,1,1,1,0,0,2,1,2,0,1,1,2,3,  
,0,0,2,1,2,3,0,0,1,0,0,2,1,1,0,0,2,1,2,0,0,1,1]

Expansion in base  $(n^2 \cdot 2^n - 1)$  of  $1/x$  :  
[0,0,11,3,0,0,0,0,1,1,1,1,1,0,2,0,1,0,0,0,0,0,1,2,0,0,1,1,1,0,0,1,2,0,0,  
,0,0,0,1,1,1,0,1,0,0,0,1,1,0,1,1,1,0,0,0,0,0,1,1,0,1,1,0,0,1,0,0,1,1,1,  
1,1,1,0,0,1,1,0,0,0,1,1,0,1,1,0,1,1,0,0,1,1,0,0,1,1,1,0,0,0,0,1,0,1,1,0,0,  
,0,1,2,0,0,0,0,1,0,1,0,0,0,0,0,1,0,1,0,0,1,0,1,1,0,1,1,0,0,0,0,1,0,1,0,  
0,1,1,0,1,0,0,0,0,0,0,0,0,1,1,2,0,0,0,0,0,1,1,0,0,1,1,0,1,1,1,1,0,0,0,  
0,0,0,0,1,1,1,1,0,0,1,0,1,1,1,1,0,0,0,1,0,0,1,0,0,0,2,0,0,0,0,0,0,0,1,  
0]

Expansion in base  $(n^2 \cdot 2^n + 1)$  of  $1/x$  :  
[0,2,5,3,2,2,2,0,0,2,0,0,2,0,0,1,1,1,0,1,1,1,1,0,0,1,1,0,2,0,0,0,1,1,1,  
2,0,0,0,1,0,0,1,0,1,1,1,0,0,0,1,0,0,0,0,0,1,1,0,1,1,0,1,1,0,0,0,0,0,1,1,  
,0,1,0,0,0,0,1,1,0,1,1,0,0,0,0,1,0,0,1,0,0,0,1,1,0,0,1,0,0,1,0,0,0,1,0,  
0,0,1,1,1,0,0,1,0,0,0,1,1,1,0,0,0,0,1,0,0,0,0,0,0,1,0,1,1,1,0,1,0,1,0,  
,0,1,0,0,0,0,1,1,0,1,1,0,1,0,1,1,1,0,1,1,1,1,0,1,1,1,0,1,1,0,0,1,0,1,  
1,1,1,1,0,0,0,0,0,1,1,1,1,1,0,0,1,1,0,1,1,1,1,1,1,1,1,1,0,1,1,0,0,0,1,1,1,  
]

Expansion in base  $(n^2 \cdot \exp(n) - 1)$  of  $1/x$  :  
[0,1,9,5,0,4,0,2,2,2,2,0,3,0,1,3,0,0,1,0,0,1,0,2,2,0,2,2,1,2,0,2,1,2,1,  
0,1,0,1,0,1,2,0,1,0,0,0,1,0,2,1,2,1,1,0,1,0,0,2,0,0,1,1,2,1,0,2,0,1,0,0,  
,0,1,1,1,0,2,0,2,1,1,1,1,1,1,1,1,0,2,2,0,1,0,0,0,2,1,2,1,2,0,1,1,1,2,  
0,1,2,0,1,2,1,2,1,2,0,2,0,0,2,1,0,0,2,2,0,0,0,2,0,1,2,2,0,0,1,0,2,0,1,0,  
,0,0,0,0,1,1]

Expansion in base  $(n^2 \cdot \exp(n) + 1)$  of  $1/x$  :  
[0,3,5,1,2,3,3,1,2,2,0,2,0,1,0,2,1,0,2,0,0,2,2,1,0,1,1,1,0,1,2,1,0,1,1,  
2,0,2,2,0,1,2,1,0,0,2,0,0,2,1,2,1,2,2,0,0,2,0,1,0,1,2,0,2,0,1,2,0,0,1,0,  
,0,1,1,0,1,0,0,0,0,1,1,2,0,0,1,0,0,2,0,1,0,2,0,2,0,0,1,1,0,1,0,2,1,2,1,  
1,0,0,1,1,0,0,0,2,1,1,1,1,0,1,1,1,1,0,0,1,0,0,0,0,1,0,2,0,1,0,0,0,2,0,0,  
,2,1,1,2,1,1]

Expansion in base  $(n^2 \cdot 10^n - 1)$  of  $1/x$  :  
[0,8,29,20,6,10,6,5,6,3,3,4,0,0,3,5,0,7,7,2,3,4,9,9,9,4,10,3,9,1,4,0,8,  
9,4,5,2,8,6,4,3,8,5,6,9,7,6,7,9,7,4,6,4,6,7,8,4,4,3,0,3,1,8,0,5]

Expansion in base  $(n^2 \cdot 10^n + 1)$  of  $1/x$  :  
[0,10,22,7,10,3,10,6,8,0,5,9,4,8,0,9,6,8,5,0,8,10,10,7,3,3,4,2,0,3,8,0,  
3,3,1,3,3,3,0,1,0,7,1,9,4,8,9,0,3,3,9,6,8,1,6,2,5,0,3,2,1,1,8,7,8]

Expansion in base  $(n^2 \cdot \exp(2\pi n) - 1)$  of  $1 - \text{frac}(x)$  :  
[0,514,1618,273,920,161,372,322,54,526,32,229,447,377,313,423,430,586,1  
37,491,190,301,454,202]

Expansion in base  $(n^2 \cdot \exp(2\pi n) + 1)$  of  $1 - \text{frac}(x)$  :  
[0,516,1454,366,587,82,643,527,549,535,100,347,303,581,51,413,528,112,4  
01,368,37,91,78,150]

Expansion in base  $(n^2 \cdot \exp(\pi n) - 1)$  of  $1 - \text{frac}(x)$  :  
[0,21,31,10,13,27,21,31,10,19,1,15,9,9,11,6,4,0,21,10,2,12,21,12,11,23,  
16,16,3,7,2,8,8,1,16,19,23,18,14,21,23,10,20,2,9,5,0]

Expansion in base  $(n^2 \cdot \exp(\pi n) + 1)$  of  $1 - \text{frac}(x)$  :  
[0,23,22,8,2,25,4,31,8,5,23,26,10,12,0,25,11,12,6,15,23,9,19,2,3,21,12,  
1,12,14,12,15,11,19,19,2,12,2,22,20,20,8,19,6,4,1,10]

Expansion in base  $(n^2 \cdot \pi^n - 1)$  of  $1 - \text{frac}(x)$  :  
[0,2,1,0,1,2,3,0,2,2,2,0,2,1,1,0,0,3,1,0,0,1,2,2,0,0,1,0,2,1,1,2,1,2,3,  
0,1,0,1,1,1,0,2,0,0,1,3,0,2,2,2,1,0,1,2,1,2,0,1,2,2,0,0,0,2,2,2,0,0,0,  
3,0,1,1,1,0,0,2,2,2,0,3,0,0,2,2,1,0,3,0,1,0,0,2,3,0,1,1,3,0,0,2,0,1,1,  
2,1,0,2,2,0,1,0,2,1,2,3,0,1,2,1,0,0,0,0,0,3,0]

Expansion in base  $(n^2 \cdot \pi^n + 1)$  of  $1 - \text{frac}(x)$  :  
[0,3,10,2,2,3,3,3,1,3,1,2,0,0,3,0,2,1,0,0,3,0,1,1,0,1,0,2,1,2,1,1,3,0,0,  
1,1,1,1,1,2,0,0,3,0,2,2,1,2,0,0,0,2,2,0,2,2,3,0,1,1,0,0,2,1,1,1,1,0,1,  
2,1,0,1,0,1,1,1,1,1,2,1,2,2,0,2,0,1,0,2,1,0,0,0,2,2,2,0,0,0,1,2,2,2,0,0,  
2,2,1,2,1,3,0,1,0,1,1,2,1,3,0,0,0,1,1,2,1,2,0]

Expansion in base  $(n^2 \cdot 2^n - 1)$  of  $1 - \text{frac}(x)$  :  
[0,0,11,2,3,1,1,2,1,1,2,0,1,0,0,1,1,1,1,0,1,1,1,2,0,0,0,0,0,1,1,1,0,1,1,  
1,1,1,0,0,1,1,0,0,0,1,1,0,0,0,0,2,0,0,0,0,0,1,0,1,1,2,0,0,0,0,1,0,1,0,  
1,1,1,0,0,1,0,0,1,0,0,1,1,0,1,0,0,0,0,1,1,1,0,0,0,0,2,0,0,0,0,0,1,1,1,0,  
1,0,1,1,1,0,2,0,0,0,0,0,0,1,0,1,1,0,1,0,0,0,0,2,0,0,0,0,1,0,0,0,0,1,0,  
1,0,1,1,0,1,0,0,0,0,0,0,0,1,1,1,0,0,1,1,0,1,0,1,0,1,1,0,1,1,1,0,1,1,  
0,0,1,1,1,0,1,0,1,0,0,1,1,1,1,0,1,0,1,0,0,0,0,1,1,0,1,1,0,0,1,0,1,1,1,  
0]

Expansion in base  $(n^2 \cdot 2^n + 1)$  of  $1 - \text{frac}(x)$  :  
[0,2,5,3,2,1,1,2,0,2,1,0,1,0,0,1,0,0,0,0,1,2,0,0,1,0,0,1,1,1,1,0,0,0,1,  
0,1,1,1,1,0,2,0,0,0,0,0,0,0,0,1,0,2,0,0,0,1,0,1,1,1,1,0,0,1,1,0,0,0,1,1,  
1,0,2,0,0,0,0,0,0,1,1,1,0,0,0,0,0,1,1,0,1,0,1,1,1,1,0,0,0,0,1,1,0,1,1,  
0,1,1,1,1,1,1,0,0,0,0,1,0,0,1,1,1,1,1,1,0,1,1,0,0,1,1,0,2,0,0,0,0,0,0,1,  
1,0,1,0,1,1,0,0,1,1,0,1,1,0,0,0,2,0,0,0,0,0,0,1,0,0,1,1,0,1,0,1,1,1,0,  
0,0,1,0,0,1,0,0,0,0,0,0,0,1,1,1,1,0,0,1,0,0,0,1,0,1,1,0,2,0,0,0,0,0,0,1,  
]

Expansion in base  $(n^2 \cdot \exp(n) - 1)$  of  $1 - \text{frac}(x)$  :  
[0,1,9,4,4,3,2,1,1,2,1,0,1,1,1,3,0,1,0,0,2,0,2,0,2,2,0,1,1,1,1,1,1,2,0,  
2,0,1,0,0,0,1,0,0,0,1,0,1,0,1,2,1,0,0,2,2,0,0,1,0,1,1,2,1,1,1,1,0,2,1,1,  
2,0,2,0,0,2,1,1,0,0,0,0,2,0,0,0,0,0,2,1,2,1,2,0,2,1,0,0,0,1,0,0,1,2,1,  
2,1,1,1,2,1,1,1,1,0,0,1,1,0,0,0,0,1,1,0,0,1,1,0,2,1,1,0,2,0,2,1,1,1,0,1,  
1,2,0,0,1,2]

Expansion in base  $(n^2 \cdot \exp(n) + 1)$  of  $1 - \text{frac}(x)$  :  
[0,3,5,1,1,3,0,2,1,3,1,0,1,1,0,0,1,1,2,2,2,2,0,0,1,0,0,1,0,0,0,1,2,1,0,  
2,1,2,0,1,1,0,1,1,2,1,0,1,1,0,1,2,2,0,0,1,1,0,1,0,2,1,1,2,0,1,2,0,1,2,0,  
1,2,2,0,0,1,0,2,1,2,0,1,2,0,1,2,1,1,1,1,1,0,1,2,0,1,0,1,2,1,0,2,1,1,1,



Expansion in base  $(n^2 \cdot \exp(n) - 1)$  of  $1/(1 - \text{frac}(x))$  :

[1,0,0,6,2,3,3,3,0,2,2,0,2,2,1,0,1,1,2,0,1,0,2,1,0,2,2,0,2,2,0,1,2,0,0,  
1,1,1,2,1,0,2,0,0,1,2,0,1,2,1,0,1,1,1,0,1,2,0,1,0,2,1,1,0,2,1,2,0,1,0,1  
,2,1,2,2,0,1,0,2,0,0,1,1,0,2,1,1,1,0,1,0,0,1,1,1,1,0,1,2,1,1,1,0,1,2,0,  
0,1,2,2,0,0,0,2,1,0,1,1,2,1,0,0,0,1,0,0,2,1,1,1,1,0,0,2,0,0,2,1,1,2,0,0  
,1,0,0,0,2,1]

Expansion in base  $(n^2 \cdot \exp(n) + 1)$  of  $1/(1 - \text{frac}(x))$  :

[1,0,1,1,2,3,3,0,3,0,0,1,2,1,0,2,1,2,0,0,0,2,1,2,1,1,1,2,2,1,2,1,1,2,0,  
0,0,0,2,1,1,1,2,2,0,2,1,2,0,1,2,1,2,2,0,0,0,0,1,0,0,2,0,0,1,2,1,1,0,0,2  
,2,0,0,2,1,2,0,0,0,1,0,1,1,2,2,0,0,0,2,1,0,0,0,2,1,1,1,2,1,0,0,2,0,1,0,  
0,2,1,1,1,0,2,1,2,0,2,1,0,1,0,2,2,0,0,1,1,0,0,0,0,2,0,1,0,0,2,0,1,2,0,0  
,2,0,1,0,2,0]

Expansion in base  $(n^2 \cdot 10^n - 1)$  of  $1/(1 - \text{frac}(x))$  :

[1,0,15,4,3,3,2,8,6,5,0,3,8,2,7,2,5,0,7,6,2,10,10,4,9,5,7,7,2,2,5,0,1,8  
,3,7,5,1,7,9,7,0,9,0,8,9,10,2,9,6,1,2,7,0,1,1,0,5,9,1,6,5,8,7,8]

Expansion in base  $(n^2 \cdot 10^n + 1)$  of  $1/(1 - \text{frac}(x))$  :

[1,0,15,10,16,12,7,1,9,12,7,8,2,4,4,11,1,6,1,8,10,6,9,3,9,0,0,1,6,7,2,2  
,2,0,6,1,9,9,6,3,2,3,3,0,6,6,2,6,4,6,7,1,10,1,0,5,4,1,5,6,7,9,6,8,4]

Expansion in base  $(n^3 \cdot \exp(2 \cdot \text{Pi} \cdot n) - 1)$  of  $x$  :

[1,19,3165,1140,890,407,276,415,342,366,398,505,218,388,308,121,216,633  
,424,423,222,300,611,243]

Expansion in base  $(n^3 \cdot \exp(2 \cdot \text{Pi} \cdot n) + 1)$  of  $x$  :

[1,19,3469,1184,544,640,338,613,199,751,399,470,669,619,340,507,182,604  
,247,547,505,179,245,591]

Expansion in base  $(n^3 \cdot \exp(\text{Pi} \cdot n) - 1)$  of  $x$  :

[1,0,157,70,25,20,5,32,26,27,29,3,6,17,19,22,3,9,5,20,18,20,19,17,17,8,  
11,3,8,21,6,3,3,17,13,17,9,9,5,6,15,20,13,3,2,11,1]

Expansion in base  $(n^3 \cdot \exp(\text{Pi} \cdot n) + 1)$  of  $x$  :

[1,0,158,38,17,11,10,4,30,31,0,24,26,14,6,27,27,12,10,11,10,16,6,11,24,  
10,3,8,3,12,11,20,0,23,9,7,10,8,0,11,22,3,21,12,23,22,1]

Expansion in base  $(n^3 \cdot \text{Pi}^n - 1)$  of  $x$  :

[1,0,2,7,0,3,4,3,2,3,2,1,2,0,1,0,1,2,1,1,2,2,0,1,2,1,3,0,1,1,0,0,1,0,1,  
0,0,1,0,1,0,0,2,2,3,0,1,0,0,2,2,2,0,2,0,1,1,2,3,0,2,2,0,1,0,3,0,0,1,1,1  
,2,1,2,2,0,3,0,1,1,1,3,0,0,0,2,1,1,2,1,0,2,1,1,0,1,0,0,0,0,1,1,3,0,1,2,  
0,2,2,2,1,0,0,0,2,1,1,0,0,1,1,1,2,1,1,1,0,1,0]

Expansion in base  $(n^3 \cdot \text{Pi}^n + 1)$  of  $x$  :

[1,0,3,2,0,4,1,4,3,0,0,1,0,2,1,1,0,0,0,1,2,0,1,2,0,2,0,2,0,0,0,0,1,2,2,  
2,2,0,0,1,2,0,0,1,1,2,0,3,0,0,2,0,3,0,0,3,1,0,0,0,3,0,0,1,2,2,0,1,0,1,2  
,2,3,0,1,1,1,1,3,0,0,2,1,1,2,2,1,1,2,0,1,0,1,0,0,2,0,3,0,2,1,2,0,0,0,0,  
1,2,3,0,1,2,0,3,0,2,0,2,2,0,1,2,0,3,0,0,0,2,2]

Expansion in base  $(n^3 \cdot 2^n - 1)$  of  $x$  :

[1,0,0,6,4,3,3,0,2,1,2,1,0,1,1,0,0,1,0,0,1,0,0,2,0,1,0,1,1,1,1,1,0,1,0,  
1,1,1,0,1,1,0,0,0,2,0,0,0,0,0,1,1,0,1,0,0,0,1,0,0,1,0,1,1,0,0,0,0,0,0,  
,0,1,0,0,1,0,0,1,0,1,0,0,1,1,1,0,0,0,0,0,1,0,2,0,0,0,0,1,1,0,1,2,0,0,0,  
1,0,0,0,0,1,1,1,1,1,0,0,1,0,0,1,1,0,1,1,0,0,0,0,1,1,0,1,1,1,2,0,0,0,0,1  
,0,1,1,1,1,1,0,0,0,1,0,0,1,1,0,1,0,0,1,1,0,1,0,1,1,1,0,2,0,0,0,0,0,1,0,  
0,1,1,1,1,1,0,1,1,0,1,1,0,0,1,1,1,0,1,0,0,0,0,1,0,0,1,0,0,1,1,1,0,0,1  
]

Expansion in base  $(n^3 \cdot 2^n + 1)$  of  $x$  :

[1,0,1,2,4,0,0,0,2,2,0,0,2,0,0,0,0,1,0,1,1,1,1,1,1,0,0,0,2,0,0,0,1,2,  
0,0,1,1,1,2,0,0,0,1,1,1,1,1,1,0,1,1,0,0,1,1,1,1,1,1,1,1,1,0,1,0,0,1,1,  
,0,0,1,1,1,0,0,1,0,1,1,0,1,1,0,1,1,0,2,0,0,0,0,0,0,0,0,1,1,0,0,1,1,0,0,  
0,0,0,1,1,0,0,0,1,1,1,0,0,1,1,0,0,0,1,0,1,1,0,1,1,1,1,0,0,0,1,1,0,1,0,1,  
,1,0,1,1,1,0,2,0,0,0,0,0,0,1,0,1,1,0,1,1,0,1,1,0,0,0,0,1,1,0,0,0,0,0,0,  
0,0,0,1,1,0,0,1,0,0,0,0,0,1,0,0,1,1,1,0,1,1,0,0,1,1,1,0,0,0,1,0,1,1,1,  
]

Expansion in base  $(n^3 \cdot \exp(n) - 1)$  of  $x$  :

[1,0,1,8,6,1,3,0,0,2,3,1,0,2,0,1,1,0,2,2,1,2,3,0,0,2,0,1,2,1,1,2,2,2,2,  
1,0,0,0,1,1,1,2,1,0,2,0,2,2,0,2,0,2,2,0,1,0,2,2,0,1,2,0,0,2,1,0,1,2,2,0,  
,0,2,2,0,1,0,0,1,1,1,1,2,2,0,0,0,1,1,0,2,0,1,0,1,0,1,0,0,0,0,0,2,0,1,2,  
1,2,2,0,0,0,1,1,0,1,0,2,0,1,0,1,0,1,1,0,2,1,2,1,1,0,0,2,0,0,1,0,1,1,0,1,  
,1,2,0,1,0,1]

Expansion in base  $(n^3 \cdot \exp(n) + 1)$  of  $x$  :

[1,0,2,4,0,1,4,0,2,1,3,1,2,2,0,0,3,0,2,2,1,0,2,0,0,1,0,2,1,2,1,0,2,1,0,  
0,2,0,0,1,1,0,1,0,1,2,2,1,0,2,2,0,0,1,0,0,0,2,2,1,0,0,0,2,0,2,2,0,1,2,1,  
,1,0,2,0,1,2,0,1,1,1,2,1,1,2,0,2,0,1,2,1,1,2,1,2,1,1,2,0,0,1,2,0,1,2,1,  
0,0,1,2,1,1,0,1,1,0,2,1,0,2,1,2,2,0,0,2,1,1,2,2,0,1,0,1,2,1,0,2,0,2,0,1,  
,0,0,2,2,0,1]

Expansion in base  $(n^3 \cdot 10^n - 1)$  of  $x$  :

[1,0,29,8,9,11,12,4,0,0,10,5,4,5,2,0,4,0,1,10,8,2,10,8,6,4,4,7,0,8,0,6,  
5,1,5,6,10,4,4,6,0,9,3,10,3,10,5,9,10,0,2,9,6,2,4,6,3,7,5,5,7,7,1,7,6]

Expansion in base  $(n^3 \cdot 10^n + 1)$  of  $x$  :

[1,0,29,28,0,8,5,6,5,7,2,0,6,1,3,2,2,2,6,5,0,6,0,9,6,4,8,6,1,5,8,6,2,7,  
9,5,10,6,9,7,6,5,10,3,1,0,6,6,7,2,4,2,5,4,2,7,5,6,9,6,3,2,5,3,8]

Expansion in base  $(n^3 \cdot \exp(2 \cdot \pi \cdot n) - 1)$  of  $1/x$  :

[0,515,1961,639,1135,479,878,428,401,692,519,395,305,28,14,248,441,603,  
499,284,9,586,125,359]

Expansion in base  $(n^3 \cdot \exp(2 \cdot \pi \cdot n) + 1)$  of  $1/x$  :

[0,517,1649,901,1237,429,22,281,334,99,309,505,292,381,219,187,481,480,  
164,280,170,380,304,440]

Expansion in base  $(n^3 \cdot \exp(\pi \cdot n) - 1)$  of  $1/x$  :

[0,21,68,1,28,43,1,2,10,10,5,28,27,7,11,13,6,18,20,7,14,14,3,5,10,20,1,  
19,24,17,1,13,3,10,5,2,17,14,14,2,14,13,20,17,16,18,19]

Expansion in base  $(n^3 \cdot \exp(\pi \cdot n) + 1)$  of  $1/x$  :

[0,23,49,74,23,18,15,10,0,5,24,10,29,6,24,1,4,18,25,7,4,7,25,21,15,11,1,  
0,23,13,20,24,6,13,9,23,13,2,18,9,4,24,8,18,5,6,14,2]

Expansion in base  $(n^3 \cdot \pi^n - 1)$  of  $1/x$  :

[0,2,2,1,6,4,1,0,1,2,1,3,0,1,0,2,3,2,2,3,2,0,3,0,0,3,1,2,2,3,0,2,1,3,0,  
1,0,2,1,3,1,0,3,0,2,3,1,0,1,0,2,0,1,0,2,2,0,2,1,0,2,1,2,0,1,1,1,0,0,0,1,  
,2,0,0,1,2,1,1,2,2,1,0,1,0,1,3,0,1,1,1,2,1,0,1,1,0,1,2,1,0,0,1,2,1,2,0,  
0,3,0,0,2,0,0,0,2,0,0,0,1,0,1,1,3,0,2,0,2,2,1]

Expansion in base  $(n^3 \cdot \pi^n + 1)$  of  $1/x$  :

[0,3,20,8,4,5,1,1,2,2,3,2,0,0,0,2,0,1,1,0,2,0,2,1,0,1,1,2,2,1,0,1,0,2,3,  
,0,1,0,1,0,0,2,0,0,1,0,1,3,0,1,1,1,1,2,0,0,1,0,0,0,1,0,0,1,1,2,0,2,1,2,  
1,0,0,0,1,0,2,1,3,0,2,1,1,1,0,1,1,1,1,2,2,2,3,0,0,1,2,2,0,0,0,1,2,0,1,1,  
,2,1,1,0,1,1,2,2,1,0,1,0,1,3,0,1,2,1,2,2,0,1,1]



3,0,2,1,0,0,1,2,1,0,2,0,0,0,2,0,3,0,2,1,1,0,1,1,0,1,1,2,2,0,1,1,1,1,3,0  
,1,3,0,1,0,2,0,2,1,3,0,2,1,2,1,1,1,0,2,2,2,2,1,1,1,2,1,2,2,2,0,0,0,1,1,  
0,1,1,0,2,3,0,2,0,0,0,3,0,0,2,0,1,0,3,0,0,1,2]

Expansion in base  $(n^3 \cdot \pi^n + 1)$  of  $1 - \text{frac}(x)$  :

[0,3,20,7,3,5,1,2,2,0,2,1,1,3,1,1,3,2,2,3,2,0,0,2,0,3,0,1,0,2,1,1,3,0,0  
,0,2,0,2,0,0,0,1,0,2,3,1,0,0,3,0,2,2,2,1,2,0,2,1,2,2,1,3,0,3,0,0,1,1,0,  
2,2,1,1,0,1,3,0,0,1,0,0,2,0,3,0,2,0,0,0,0,0,2,0,2,2,2,0,0,0,2,0,2,0,2  
,0,1,1,2,1,2,1,2,0,1,1,0,0,0,1,1,3,0,0,0,0,0,2]

Expansion in base  $(n^3 \cdot 2^n - 1)$  of  $1 - \text{frac}(x)$  :

[0,0,23,0,4,2,0,2,1,0,2,1,1,1,1,0,0,1,1,1,1,1,1,0,1,0,0,1,0,0,0,1,0,0,1  
,0,0,0,1,0,0,1,0,0,0,0,1,1,0,1,0,1,2,0,0,0,1,0,0,0,0,0,1,1,0,1,0,1,0,0,  
0,0,1,1,1,0,0,0,0,0,0,1,0,1,1,0,1,0,0,0,0,1,0,1,1,1,1,0,1,0,0,1,1,0,0,1  
,0,0,1,0,0,1,1,1,1,1,0,0,0,1,2,0,0,0,0,0,1,0,0,0,1,1,1,0,1,1,0,0,0,0,  
0,0,1,0,1,1,1,1,0,0,0,0,0,1,1,2,0,0,0,0,0,1,1,0,0,0,0,0,1,0,0,0,0,1,1  
,0,0,0,0,1,0,1,0,1,0,1,0,0,1,0,0,0,0,1,0,1,1,0,1,1,0,1,0,0,0,0,0,1,1,0,  
1]

Expansion in base  $(n^3 \cdot 2^n + 1)$  of  $1 - \text{frac}(x)$  :

[0,2,11,5,0,3,1,1,1,0,0,2,0,0,0,1,1,1,1,0,2,0,1,1,0,0,1,0,2,0,0,0,0,1,0  
,1,1,1,0,1,0,0,0,0,1,1,1,0,1,1,0,2,0,0,0,1,1,1,0,1,0,1,0,0,0,1,0,0,2,0,  
0,0,0,0,1,1,1,0,0,2,0,0,0,0,0,1,0,0,0,0,1,0,0,0,1,0,1,0,1,0,0,1,0,0,1,1  
,2,0,0,0,0,1,1,0,1,0,0,1,0,0,1,1,0,1,0,1,1,0,1,0,1,0,1,0,0,0,0,1,0,0,1,  
1,0,0,0,1,0,0,0,0,1,0,0,1,1,1,0,0,1,0,2,0,0,0,0,0,1,1,2,0,0,0,0,0,1,1,0  
,0,1,1,1,0,1,0,1,1,0,0,0,0,0,1,1,1,0,0,1,0,0,1,0,0,0,1,1,2,0,0,0,0,0,  
0]

Expansion in base  $(n^3 \cdot \exp(n) - 1)$  of  $1 - \text{frac}(x)$  :

[0,1,19,4,5,2,3,1,0,2,3,1,1,1,2,1,0,0,2,2,1,0,0,0,2,2,0,2,1,2,2,0,1,2,0  
,0,1,0,0,0,2,0,2,2,1,1,1,1,1,0,0,2,0,1,0,0,1,1,2,0,2,0,2,2,0,1,2,1,0,1,  
1,2,0,2,0,0,0,1,1,1,2,1,2,2,0,0,0,0,2,0,0,0,2,1,2,1,1,0,0,2,0,2,0,1,1,2  
,0,2,0,0,1,2,0,0,2,0,0,0,1,1,2,2,0,1,1,0,0,2,1,0,0,0,0,1,2,1,1,0,2,1,0,  
2,1,0,0,1,1,0]

Expansion in base  $(n^3 \cdot \exp(n) + 1)$  of  $1 - \text{frac}(x)$  :

[0,3,10,4,0,4,0,1,2,0,2,3,2,0,0,0,2,1,0,2,1,1,0,0,0,1,1,2,2,1,0,0,0,0,0  
,0,1,0,2,0,2,1,1,1,2,0,2,1,0,0,1,1,2,0,0,0,1,1,1,1,0,1,1,0,2,2,0,2,2,0,  
2,2,0,1,0,2,1,0,1,0,1,0,1,2,1,0,0,1,0,1,2,1,0,0,0,2,0,2,0,1,2,2,0,0,0,0  
,2,1,2,0,0,2,0,0,1,2,2,0,1,1,1,0,0,0,2,0,1,2,1,1,2,1,0,0,1,0,2,1,2,1,1,  
2,1,0,1,2,0,0]

Expansion in base  $(n^3 \cdot 10^n - 1)$  of  $1 - \text{frac}(x)$  :

[0,8,58,25,15,9,4,5,6,8,11,0,7,5,1,2,11,5,11,6,6,2,1,9,0,1,7,10,4,4,4,1  
,3,5,6,4,6,3,4,3,8,8,5,2,5,0,3,7,1,6,4,8,4,8,10,5,0,1,5,4,9,4,7,1,1]

Expansion in base  $(n^3 \cdot 10^n + 1)$  of  $1 - \text{frac}(x)$  :

[0,10,43,20,15,0,16,13,11,5,12,9,0,11,3,1,4,0,7,2,5,4,4,1,4,1,9,1,5,5,0  
,0,4,10,9,4,6,3,0,2,5,2,2,4,10,3,7,6,1,7,10,0,5,10,5,4,5,8,7,4,1,5,5,3,  
10]

Expansion in base  $(n^3 \cdot \exp(2 \cdot \pi \cdot n) - 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,20,2121,1596,977,606,160,145,22,12,691,178,486,525,583,141,292,379,4  
79,12,355,400,445,444]

Expansion in base  $(n^3 \cdot \exp(2 \cdot \pi \cdot n) + 1)$  of  $1 / (1 - \text{frac}(x))$  :

[1,20,2441,1627,684,926,655,583,258,453,162,290,554,371,332,67,535,501,  
58,489,289,149,98,195]

Expansion in base  $(n^3 \exp(\pi n) - 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,163,74,39,40,38,1,5,30,30,24,28,23,5,23,9,13,1,1,1,14,17,17,2,16,1  
2,2,5,13,7,3,21,21,5,1,18,23,20,17,20,4,16,22,13,3,9]

Expansion in base  $(n^3 \exp(\pi n) + 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,164,44,18,2,10,8,10,6,28,5,4,14,28,15,3,27,15,7,4,9,21,7,15,18,19,  
19,11,3,8,3,20,13,7,9,0,24,21,10,14,13,4,4,14,15,14]

Expansion in base  $(n^3 \pi^n - 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,2,8,1,4,3,1,3,1,0,1,0,1,1,1,0,3,1,0,2,3,0,0,1,0,0,2,2,0,0,1,1,1,0,  
0,2,2,2,0,2,2,2,3,0,1,0,2,2,0,3,0,0,1,2,2,0,1,0,2,0,0,0,1,2,1,0,0,1,0,0,  
2,2,2,0,2,1,0,1,3,0,0,0,1,2,1,1,0,1,2,2,0,0,0,0,2,0,0,1,2,3,0,1,2,0,2,  
2,1,0,2,2,0,0,1,1,2,1,2,2,1,1,2,2,0,2,2,1,3,0]

Expansion in base  $(n^3 \pi^n + 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,3,3,2,2,0,2,3,1,2,1,2,3,3,1,0,1,0,1,1,1,0,1,2,3,0,1,1,0,2,3,1,1,2,  
2,2,1,3,0,1,1,1,2,0,2,2,1,1,1,1,0,1,0,0,3,0,0,1,1,3,0,2,0,0,0,3,0,1,2,1,  
0,1,3,0,0,2,0,2,2,1,2,0,0,0,0,1,2,2,1,2,0,0,0,2,0,2,1,2,1,2,0,2,0,3,0,  
2,0,2,1,2,3,0,0,2,1,0,0,2,0,2,2,1,2,1,3,0,1,0]

Expansion in base  $(n^3 2^n - 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,0,7,1,1,0,0,0,2,1,1,1,1,1,0,0,0,1,2,0,0,0,1,1,0,1,2,0,0,0,1,1,  
0,0,0,1,0,0,1,1,2,0,0,0,1,1,0,1,0,1,0,0,1,1,1,1,0,1,0,0,0,1,0,0,0,0,1,0,  
1,0,1,1,0,1,2,0,0,0,1,0,0,1,0,0,1,1,1,1,0,0,0,0,1,1,0,0,1,0,1,0,0,1,0,  
1,1,0,2,0,0,0,0,0,1,1,0,0,1,1,0,0,0,1,0,0,1,1,1,0,0,1,1,0,0,1,1,0,2,0,0,0,0,0,  
1,1,0,2,0,0,0,0,0,1,0,0,0,0,0,1,1,0,1,1,1,0,0,1,0,0,1,1,1,0,0,1,0,1,0,  
0,1,1,0,1,1,0,0,1,0,1,1,0,0,0,1,0,0,0,1,2,0,0,0,0,0,0,0,1,1,0,1,0,0,0,0,1  
]

Expansion in base  $(n^3 2^n + 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,1,3,1,0,1,0,1,0,0,0,0,1,1,0,0,1,1,1,2,0,0,2,0,1,0,1,0,0,0,0,0,0,1,  
1,0,0,1,1,1,1,1,0,0,1,2,0,0,0,0,1,1,0,0,0,1,1,0,0,0,1,0,1,1,0,0,1,0,0,0,  
1,1,2,0,0,0,0,1,1,1,1,0,1,1,1,0,0,1,2,0,0,0,0,1,0,1,1,1,2,0,0,0,0,1,1,  
1,0,1,0,1,0,1,1,0,0,0,0,0,1,1,2,0,0,0,0,0,0,1,0,0,1,0,0,0,0,1,1,1,0,0,0,  
1,1,0,0,0,0,1,0,1,0,0,0,0,0,1,0,0,0,0,1,0,1,1,1,0,0,1,0,1,1,1,1,0,0,1,  
1,1,1,0,0,0,0,1,0,1,1,1,0,0,0,1,0,1,1,1,1,0,0,0,1,0,1,0,0,0,0,1,0,1,1,0  
]

Expansion in base  $(n^3 \exp(n) - 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,1,9,4,2,3,1,3,0,0,0,0,1,0,0,1,2,0,2,2,1,0,0,1,2,2,2,2,2,0,0,2,0,2,  
1,2,0,1,2,2,0,2,1,1,0,0,0,0,0,0,1,2,0,1,0,1,1,0,1,0,1,0,2,0,1,2,0,1,1,0,  
1,0,0,1,0,1,2,1,1,1,2,2,0,1,0,1,2,0,1,2,2,0,1,1,2,0,0,1,0,1,2,1,0,0,0,  
0,1,1,1,2,2,0,1,0,1,2,1,1,2,0,1,0,0,2,0,0,1,0,2,0,0,2,1,1,0,1,1,1,1,1,2,  
1,0,2,1,1,1]

Expansion in base  $(n^3 \exp(n) + 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,2,4,5,2,0,1,3,0,0,2,3,1,0,0,2,0,2,2,1,3,0,0,1,1,2,2,0,2,2,1,0,0,0,  
0,0,1,2,1,0,0,2,1,0,0,1,1,1,2,0,0,2,1,1,2,1,2,2,0,1,0,2,1,0,0,0,1,0,1,2,  
0,0,2,0,2,0,2,0,0,0,2,0,1,0,2,0,1,2,1,2,2,0,2,0,0,2,0,1,1,0,2,0,0,0,1,  
0,1,1,1,2,0,0,0,1,1,2,1,0,0,0,2,1,0,0,0,2,1,2,1,2,0,2,0,2,1,0,2,1,0,2,1,  
1,0,2,0,1,2]

Expansion in base  $(n^3 10^n - 1)$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,30,12,12,15,15,11,11,11,2,4,4,4,11,7,8,2,11,8,0,9,8,1,9,9,9,5,6,2,  
7,3,7,0,8,7,1,0,7,7,10,3,5,3,5,5,8,1,0,10,4,10,4,8,10,1,8,1,7,4,6,2,0,6,  
1]

Expansion in base  $(n^3 \cdot 10^n + 1)$  of  $1/(1 - \text{frac}(x))$  :

[1,0,30,32,19,16,5,0,13,3,12,6,6,5,0,10,6,1,5,7,3,3,8,10,0,4,5,5,7,9,0,  
5,8,4,10,1,8,7,8,8,4,9,6,10,4,9,5,3,1,8,4,5,2,3,2,9,7,9,4,6,5,4,2,8,4]

Expansion in base  $(n/(\exp(2\pi \cdot n) - 1))$  of  $x$  :

[1,19,197,304,56,393,309,65,346,380,295,463,21,450,194,117,159,490,74,3  
34,456,88,273,113]

Expansion in base  $(n/(\exp(2\pi \cdot n) + 1))$  of  $x$  :

[1,19,216,304,272,394,166,413,354,332,378,126,89,296,89,421,422,248,399  
,129,108,116,412,293]

Expansion in base  $(n/(\exp(\pi \cdot n) - 1))$  of  $x$  :

[1,0,9,13,7,7,11,5,10,10,2,7,20,19,10,17,20,12,3,7,1,13,11,14,10,16,18,  
9,3,12,17,0,2,16,12,8,15,14,9,5,17,22,0,11,13,9,3]

Expansion in base  $(n/(\exp(\pi \cdot n) + 1))$  of  $x$  :

[1,0,9,13,16,8,5,0,13,14,19,9,12,14,16,4,4,0,18,11,14,18,11,13,7,17,17,  
3,9,11,9,5,10,22,9,2,8,18,21,8,14,18,4,18,19,13,20]

Expansion in base  $(n/(\pi^n - 1))$  of  $x$  :

[1,0,0,0,0,2,0,1,2,0,1,0,2,1,0,1,2,0,1,2,2,1,0,1,2,1,0,1,2,1,1,  
0,2,2,0,0,0,0,2,2,2,2,0,1,0,2,3,0,0,2,0,0,2,0,2,2,1,2,0,0,0,2,2,1,0,0,0,  
0,2,0,2,0,2,1,2,0,2,1,0,2,1,2,0,1,0,0,0,2,3,0,0,2,0,0,0,1,1,2,2,2,2,  
2,1,2,1,0,0,1,0,2,1,0,0,1,1,0,1,2,2,1,2,0,0,1]

Expansion in base  $(n/(\pi^n + 1))$  of  $x$  :

[1,0,0,0,0,2,0,1,2,1,0,1,1,0,0,2,1,1,1,1,0,2,0,0,1,0,1,2,1,0,1,0,2,0,0,  
0,0,0,1,1,1,0,2,2,1,2,2,1,1,0,1,2,2,0,0,0,1,1,1,0,2,1,2,2,2,1,1,2,1,0,2,  
,2,1,0,0,1,2,0,2,2,2,2,2,0,1,0,2,2,0,0,1,2,1,0,2,2,2,1,0,0,0,0,1,0,0,  
0,1,0,1,2,2,1,0,1,1,2,1,2,1,2,0,1,0,2,0,2,0,0]

Expansion in base  $(n/(2^n - 1))$  of  $x$  :

[1,0,0,0,0,0,0,0,1,0,0,1,0,0,0,0,0,1,0,1,0,1,1,0,0,0,0,1,0,1,1,0,0,1,1,  
0,0,1,0,1,0,1,0,0,0,1,0,1,0,1,1,1,0,0,0,1,1,0,1,1,0,1,0,1,1,0,0,1,1,0,1,  
,1,0,0,1,0,1,0,1,1,1,0,1,0,0,1,1,0,0,1,1,1,1,0,0,1,0,1,0,0,0,0,1,1,0,0,  
1,0,1,1,0,1,0,1,0,1,1,1,0,0,1,1,0,1,0,0,1,0,1,0,1,1,1,0,1,0,1,1,1,0,1,0,  
,0,1,1,1,0,1,0,0,1,1,0,0,0,1,0,1,0,0,0,0,0,0,0,1,0,1,0,1,0,1,0,0,1,1,0,  
0,0,1,1,0,0,1,1,0,1,1,1,1,0,0,1,1,0,1,1,0,1,0,0,0,1,1,0,0,1,1,0,1,0,0  
]

Expansion in base  $(n/(2^n + 1))$  of  $x$  :

[1,0,0,0,0,0,0,0,1,0,0,1,0,0,0,0,1,1,0,0,0,1,0,0,1,0,1,1,1,0,0,0,  
1,0,1,0,0,1,0,1,1,0,0,0,1,1,1,0,0,1,0,1,1,0,0,0,0,0,1,0,1,0,0,0,1,0,1,1,  
,1,0,1,1,0,0,1,1,1,0,0,0,0,1,1,0,0,0,0,0,0,0,0,0,1,1,1,0,0,1,1,1,0,0,0,  
1,0,0,1,0,0,0,1,1,1,0,0,0,0,0,1,0,0,1,1,0,1,1,1,1,0,0,1,1,0,0,0,1,0,0,  
,0,1,0,1,1,1,0,0,1,0,1,1,0,1,0,1,1,0,1,1,0,1,0,1,0,1,1,1,1,0,0,0,1,1,  
0,1,0,0,1,0,0,0,1,0,1,1,0,0,1,1,0,0,0,1,0,1,0,0,1,1,0,0,0,1,1,0,0,1,0,0  
]

Expansion in base  $(n/(\exp(n) - 1))$  of  $x$  :

[1,0,0,0,0,1,0,0,1,0,0,1,1,2,0,1,2,0,0,2,0,0,0,2,0,0,2,0,0,2,0,1,1,0,  
1,0,0,2,1,1,2,0,1,0,1,1,0,0,2,1,0,2,0,1,0,2,0,0,1,1,0,2,0,1,0,2,0,1,0,1,  
,1,1,2,0,0,1,0,1,2,0,2,0,1,1,0,1,0,0,2,1,0,1,0,2,1,0,2,0,1,0,2,1,1,1,  
0,1,0,2,1,1,2,0,1,2,0,1,1,0,1,0,2,0,0,0,1,1,1,2,1,0,1,2,1,0,1,2,1,1,0,0,  
,2,0,2,0,1,0]

Expansion in base  $(n/(\exp(n) + 1))$  of  $x$  :

[1,0,0,0,0,1,0,0,1,0,1,1,1,2,0,2,0,1,2,0,1,2,0,1,2,0,1,2,0,1,1,1,1,2,0,  
0,2,0,0,1,1,0,1,0,1,0,1,1,0,2,0,0,2,1,0,1,1,2,0,2,1,0,1,2,0,0,0,1,2,0,0,  
,0,2,1,1,0,1,1,1,2,0,1,2,0,0,1,2,0,2,0,0,0,1,0,1,2,0,0,1,2,1,0,0,0,2,1,  
0,0,2,0,1,1,0,0,1,0,1,2,1,1,1,2,1,0,2,1,0,1,2,0,0,1,1,2,0,2,0,1,0,0,2,1,  
,1,0,1,2,0,0]

Expansion in base  $(n/(10^n - 1))$  of  $x$  :

[1,0,1,5,4,2,1,6,4,4,2,8,1,9,1,3,9,2,7,0,3,8,7,8,1,6,4,7,3,1,8,8,6,8,0,  
8,0,9,4,1,7,9,3,3,5,2,1,0,0,9,1,4,2,9,6,5,8,4,8,2,1,3,8,9,7]

Expansion in base  $(n/(10^n + 1))$  of  $x$  :

[1,0,1,5,5,2,6,7,0,6,6,8,8,0,5,7,7,5,5,9,3,4,5,4,8,8,5,3,9,4,7,6,5,2,3,  
7,8,6,1,4,2,8,1,0,1,2,3,2,0,1,5,0,0,7,5,8,7,0,1,6,8,5,9,4,2]

Expansion in base  $(n/(\exp(2\pi n) - 1))$  of  $1/x$  :

[0,515,122,208,285,64,172,445,370,393,17,203,2,31,189,338,346,187,486,6  
7,259,42,266,203]

Expansion in base  $(n/(\exp(2\pi n) + 1))$  of  $1/x$  :

[0,517,103,33,179,321,365,24,177,233,203,470,3,462,314,317,425,0,190,30  
4,105,124,468,164]

Expansion in base  $(n/(\exp(\pi n) - 1))$  of  $1/x$  :

[0,21,4,3,15,5,17,3,17,17,12,9,9,8,9,14,7,5,4,6,14,5,19,3,21,21,14,1,5,  
15,19,18,19,14,0,21,2,10,12,13,20,5,17,19,4,9,15]

Expansion in base  $(n/(\exp(\pi n) + 1))$  of  $1/x$  :

[0,23,3,1,15,5,8,15,7,14,4,3,14,14,2,11,17,8,8,6,0,17,4,19,14,11,20,4,2  
,11,8,20,12,22,0,3,19,18,15,1,19,15,17,19,22,9,19]

Expansion in base  $(n/(\pi^n - 1))$  of  $1/x$  :

[0,2,0,0,0,1,2,0,1,2,1,1,1,2,1,1,2,0,0,1,0,2,1,1,1,2,2,0,2,1,3,0,0,0,2,  
1,1,1,0,0,2,0,2,0,1,0,0,2,0,2,1,1,1,0,2,2,2,2,2,1,2,2,2,0,2,1,3,0,0,2,1  
,1,1,1,0,2,1,2,0,2,2,1,1,2,1,0,0,1,0,1,1,0,3,0,0,0,1,1,2,0,1,1,0,0,0,2,  
1,2,0,1,0,1,2,1,2,2,1,2,0,0,3,0,0,0,2,2,0,3,0]

Expansion in base  $(n/(\pi^n + 1))$  of  $1/x$  :

[0,3,1,0,1,0,2,1,0,1,2,2,0,1,1,0,1,0,1,1,2,2,0,0,1,1,1,0,2,0,1,0,0,3,0,  
0,1,0,1,0,2,0,2,0,0,0,2,2,1,1,1,1,1,1,1,1,2,1,2,1,1,0,2,2,1,0,2,1,0,2,1  
,1,1,1,0,1,0,0,0,0,1,2,1,1,2,1,1,0,1,2,1,1,2,1,2,2,0,2,2,0,0,1,1,0,2,2,  
2,0,1,2,2,1,0,1,1,1,1,1,2,1,2,0,2,0,1,2,1,0,3]

Expansion in base  $(n/(2^n - 1))$  of  $1/x$  :

[0,0,1,0,1,0,0,0,0,1,1,0,1,0,0,0,1,1,0,0,0,1,1,0,1,1,0,1,1,1,0,1,0,0,1,1,  
0,1,0,0,0,1,0,0,1,0,0,1,0,1,1,1,0,0,0,1,1,0,0,1,1,1,0,1,0,0,0,0,1,0,0,  
,1,0,1,0,1,0,0,1,1,1,1,1,0,0,0,0,0,1,0,1,0,1,0,1,1,0,1,0,0,0,0,0,1,1,1,  
0,0,0,1,0,0,1,0,0,1,1,1,0,1,1,0,1,1,0,0,0,1,0,1,0,1,1,1,0,0,1,1,0,0,1,0  
,0,0,1,0,1,0,0,0,0,0,0,0,0,1,1,1,0,0,0,0,0,0,1,0,0,0,1,0,0,0,1,0,1,1,1,  
0,0,1,1,0,1,0,0,0,1,0,1,0,1,0,0,0,0,0,1,0,0,1,0,1,1,1,0,0,0,0,0,0,0,0  
]

Expansion in base  $(n/(2^n + 1))$  of  $1/x$  :

[0,2,0,0,1,0,0,1,0,0,0,1,0,1,1,0,1,0,1,1,0,0,0,1,1,0,0,0,1,0,1,0,1,1,0,  
0,1,0,1,1,1,0,1,0,1,0,1,1,0,0,0,0,1,1,1,1,0,1,0,1,1,0,0,0,1,0,1,0,0,0,1  
,1,0,1,1,1,0,0,1,0,1,0,0,0,0,0,1,1,1,0,0,1,0,1,0,0,1,1,0,0,0,1,1,0,0,0,1,  
1,0,1,1,0,1,1,0,0,0,1,1,0,1,1,0,0,1,0,1,0,1,0,1,1,1,0,0,0,1,0,1,1,1,0,0  
,0,0,0,0,1,1,1,0,0,0,0,1,0,0,1,0,1,1,1,0,0,1,1,0,0,1,0,0,1,0,0,1,0,0,1,  
0,0,1,0,0,1,

1,0,1,0,1,1,1,0,1,1,0,0,1,0,1,1,0,1,0,1,0,0,0,1,0,0,1,0,0,0,1,1,1,1,0,1  
]

Expansion in base  $(n/(\exp(n) - 1))$  of  $1/x$  :

[0,1,1,0,0,2,0,0,0,1,0,2,0,2,0,0,0,2,1,0,1,2,1,0,0,1,1,0,0,2,0,2,0,1,0,  
2,1,1,0,1,1,0,0,1,0,1,0,0,0,1,2,0,0,0,2,0,1,2,1,0,2,0,0,2,0,0,0,2,0,1  
,0,0,0,2,0,1,1,2,1,1,2,0,1,1,1,2,1,0,0,2,1,0,2,0,0,2,1,0,1,0,0,1,2,1,1,  
0,1,2,1,0,2,1,0,0,1,0,0,2,1,1,2,0,1,0,1,2,0,0,0,0,2,0,1,0,2,0,0,1,1,2,0  
,0,1,0,1,1,2]

Expansion in base  $(n/(\exp(n) + 1))$  of  $1/x$  :

[0,3,0,1,0,0,1,0,0,0,0,2,1,0,0,1,2,0,1,0,2,0,1,1,1,2,0,2,1,1,0,0,1,2,1,  
1,0,0,1,1,0,0,0,0,0,0,1,2,0,0,1,1,1,1,0,0,1,0,0,0,2,0,0,0,1,1,2,1,0,1,0  
,1,1,1,2,1,0,2,0,0,1,1,2,1,1,1,0,1,1,1,1,1,0,1,0,0,2,0,0,0,0,1,1,1,2,1,  
2,0,0,2,1,1,2,1,0,0,2,0,2,0,0,1,2,1,1,1,2,1,1,0,0,0,0,0,2,1,1,1,1,1  
,1,1,1,0,2,0]

Expansion in base  $(n/(10^n - 1))$  of  $1/x$  :

[0,8,3,4,7,1,5,0,1,2,0,3,2,7,8,4,7,6,4,6,2,1,4,7,5,3,2,6,1,0,1,3,6,8,4,  
5,8,0,7,9,6,4,5,6,7,0,6,6,0,0,3,5,0,8,1,5,4,8,3,2,5,0,6,6,7]

Expansion in base  $(n/(10^n + 1))$  of  $1/x$  :

[0,10,2,5,1,6,1,2,1,2,0,8,6,5,6,4,6,2,2,8,1,4,5,7,9,4,1,0,2,2,2,3,2,4,6  
,7,5,3,9,5,4,6,2,8,4,5,8,7,2,0,7,1,0,0,3,7,7,1,7,4,0,6,2,2,1]

Expansion in base  $(n/(\exp(2\pi n) - 1))$  of  $1-\text{frac}(x)$  :

[0,514,202,99,158,416,411,334,175,310,264,84,412,458,41,409,414,348,330  
,163,30,365,232,364]

Expansion in base  $(n/(\exp(2\pi n) + 1))$  of  $1-\text{frac}(x)$  :

[0,516,181,281,129,359,439,23,170,463,315,62,490,321,110,393,72,272,396  
,129,285,459,153,453]

Expansion in base  $(n/(\exp(\pi n) - 1))$  of  $1-\text{frac}(x)$  :

[0,21,3,13,15,13,6,3,2,0,5,11,20,10,5,15,9,11,5,18,13,7,8,6,15,15,10,21  
,15,13,8,14,10,15,10,2,14,20,8,14,14,8,3,9,19,15,15]

Expansion in base  $(n/(\exp(\pi n) + 1))$  of  $1-\text{frac}(x)$  :

[0,23,2,11,14,13,7,14,11,2,7,9,8,11,18,5,13,14,20,0,11,2,5,15,7,22,4,8,  
10,21,22,0,9,2,11,4,6,21,22,7,14,5,16,17,15,13,19]

Expansion in base  $(n/(\pi^n - 1))$  of  $1-\text{frac}(x)$  :

[0,2,0,0,0,1,2,0,0,0,2,2,0,2,2,0,0,2,1,0,0,2,0,1,2,2,1,2,2,2,0,0,1,0,0,  
1,2,2,2,1,1,1,1,1,1,0,0,0,2,2,2,1,2,1,1,1,1,2,0,1,0,1,1,0,0,2,0,2,3,0,0  
,1,1,1,1,0,2,0,2,1,1,2,2,0,1,0,0,1,3,0,0,2,2,2,1,2,3,0,0,2,1,2,1,1,2,1,  
1,2,2,0,1,0,2,2,2,3,0,0,1,1,2,3,0,0,0,0,3,0,0]

Expansion in base  $(n/(\pi^n + 1))$  of  $1-\text{frac}(x)$  :

[0,3,1,0,1,0,2,0,1,2,1,1,0,1,1,2,1,0,0,0,2,0,0,0,1,1,1,2,2,0,0,1,2,1,2,  
0,2,1,2,3,0,0,1,0,1,0,2,2,2,0,1,0,0,1,0,2,1,2,1,2,1,0,0,2,2,2,0,2,2,0,1  
,2,2,1,1,1,2,2,1,0,0,0,1,0,1,1,2,1,0,0,3,0,0,1,0,2,2,1,0,0,2,0,2,0,0,2,  
1,0,0,2,0,2,1,0,2,2,2,2,0,1,0,1,1,1,2,2,2,2,1]

Expansion in base  $(n/(2^n - 1))$  of  $1-\text{frac}(x)$  :

[0,0,1,0,1,0,0,0,0,1,1,0,0,1,0,1,1,0,0,1,1,0,1,0,1,0,0,0,1,1,1,0,1,0,1,  
1,1,0,0,0,1,0,1,0,0,0,0,1,0,1,0,0,0,1,0,0,1,1,1,0,1,0,1,0,0,0,1,1,1,0,0  
,1,0,0,1,1,1,0,0,1,0,0,1,1,0,0,1,1,1,1,0,0,0,0,1,1,1,0,1,1,1,0,1,0,1,  
1,1,0,1,1,0,1,0,0,1,0,1,0,1,1,1,1,1,0,1,1,0,1,1,0,1,0,0,1,1,0,1,1,1,0,0]

,1,1,0,1,1,0,0,0,0,0,1,0,1,0,0,0,1,1,0,0,0,0,1,1,0,1,0,1,0,0,1,0,0,1,0,  
0,0,0,1,0,1,1,0,1,0,1,1,1,1,1,0,0,1,0,0,0,1,0,0,1,1,1,0,0,0,1,1,0,1,1,1  
]

Expansion in base  $(n/(2^n + 1))$  of  $1 - \text{frac}(x)$  :  
[0,2,0,0,1,0,0,1,0,0,0,1,0,0,1,1,0,1,0,1,0,0,0,0,0,1,1,0,1,1,0,0,0,0,1,  
1,0,1,0,1,1,1,0,1,1,0,1,1,0,0,1,0,1,0,0,1,1,1,1,0,1,1,0,1,0,1,0,0,0,0,  
,1,1,0,0,0,1,0,0,0,1,1,1,1,0,1,0,0,0,0,1,1,0,0,1,1,1,0,1,1,0,1,0,1,0,0,  
1,0,1,1,1,1,1,0,1,0,1,1,1,0,1,1,0,0,1,1,1,0,1,0,0,0,1,1,1,0,1,1,1,0,1,0,  
,0,0,0,1,0,1,0,1,1,1,1,0,0,0,1,0,0,1,0,1,0,1,1,1,0,0,1,1,0,1,0,1,1,0,1,  
0,1,0,1,0,0,1,0,1,1,1,1,0,1,0,1,1,1,0,0,1,0,0,0,1,0,1,0,0,0,1,0,1,0,0,0,1,1  
]

Expansion in base  $(n/(\exp(n) - 1))$  of  $1 - \text{frac}(x)$  :  
[0,1,1,0,0,2,0,0,0,0,0,1,0,1,0,2,0,2,0,0,0,0,2,0,0,1,0,0,1,1,0,0,0,1,0,  
0,0,2,1,1,1,1,0,2,1,1,1,2,0,1,1,2,0,1,2,0,2,1,1,2,0,2,0,2,0,1,1,0,1,2,0,  
,1,1,2,0,1,1,1,2,1,1,0,2,1,0,1,0,2,0,1,1,0,1,0,0,0,2,0,1,0,2,1,0,1,1,1,  
0,0,1,1,0,1,1,2,0,2,0,2,1,0,1,0,1,0,1,1,2,1,0,1,2,1,0,1,1,0,0,0,1,2,0,0,  
,1,0,2,0,0,1]

Expansion in base  $(n/(\exp(n) + 1))$  of  $1 - \text{frac}(x)$  :  
[0,3,0,1,0,0,0,2,0,1,0,0,1,1,0,0,1,0,0,1,1,1,2,1,0,0,1,1,0,2,1,0,0,0,2,  
1,1,0,2,1,1,0,1,2,1,0,0,0,0,1,1,0,0,2,1,0,1,0,0,0,0,1,1,2,0,0,1,0,2,0,1,  
,2,1,1,2,0,0,0,2,0,1,1,0,2,0,2,0,2,0,1,0,0,1,0,2,1,0,0,1,1,1,0,1,0,1,1,  
1,0,0,2,1,2,0,0,2,0,0,1,2,0,0,2,0,2,1,0,2,1,1,0,1,1,1,1,0,2,1,0,2,0,0,0,  
,2,0,2,0,0,2]

Expansion in base  $(n/(10^n - 1))$  of  $1 - \text{frac}(x)$  :  
[0,8,3,4,3,7,2,4,4,4,3,7,4,5,6,0,5,6,5,4,1,4,7,8,3,2,9,0,4,8,1,2,4,5,9,  
1,9,5,9,5,7,0,7,1,7,4,8,5,3,7,5,4,7,3,8,1,2,8,1,5,2,6,9,6,1]

Expansion in base  $(n/(10^n + 1))$  of  $1 - \text{frac}(x)$  :  
[0,10,2,4,5,7,6,5,0,7,3,8,1,4,5,5,7,1,2,6,4,0,5,0,1,0,1,9,5,4,8,1,6,9,0,  
,1,3,0,8,1,1,8,9,2,0,4,5,6,3,7,2,7,1,6,2,7,5,1,6,0,7,2,7,1,0]

Expansion in base  $(n/(\exp(2\pi n) - 1))$  of  $1/(1 - \text{frac}(x))$  :  
[1,20,132,220,210,68,193,36,322,221,293,472,459,354,410,6,23,58,455,141,  
,265,355,117,45]

Expansion in base  $(n/(\exp(2\pi n) + 1))$  of  $1/(1 - \text{frac}(x))$  :  
[1,20,152,220,362,68,413,37,215,433,228,37,336,344,305,116,423,207,342,  
124,121,373,135,270]

Expansion in base  $(n/(\exp(\pi n) - 1))$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,10,3,14,4,7,18,8,18,4,15,0,7,14,19,18,13,0,19,14,20,19,21,5,10,9,1,  
7,7,18,11,15,17,9,5,16,5,12,15,22,3,1,3,2,9,22,3]

Expansion in base  $(n/(\exp(\pi n) + 1))$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,10,4,6,16,10,2,14,2,15,0,9,2,10,20,15,6,21,8,4,9,19,4,6,21,3,9,4,2,  
0,14,21,11,9,11,11,4,22,9,12,18,20,18,8,9,3,21]

Expansion in base  $(n/(\pi^n - 1))$  of  $1/(1 - \text{frac}(x))$  :  
[1,0,0,0,0,2,0,2,1,0,0,2,0,0,2,1,2,2,1,1,0,0,0,0,2,1,1,2,0,1,1,1,2,1,1,  
2,0,1,0,1,0,1,0,0,0,0,1,0,1,2,1,1,2,0,2,0,1,2,2,2,2,1,0,2,1,1,1,2,2,1,2,  
,2,0,0,0,1,1,0,2,2,2,0,2,2,1,2,1,1,2,2,2,1,0,0,2,1,2,1,1,2,3,0,0,2,2,2,  
1,1,2,1,0,0,0,2,1,2,2,2,0,1,1,1,1,1,0,3,0,0,2]

Expansion in base  $(n/(\pi^n + 1))$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,0,2,0,2,1,0,2,2,0,1,1,2,1,1,2,1,1,2,1,0,1,0,1,1,1,0,2,0,1,1,1,  
1,2,2,0,2,2,1,0,0,0,1,2,0,1,2,1,2,0,0,2,1,1,1,2,0,2,2,2,0,1,0,0,1,2,0,2  
,0,1,0,0,0,0,2,0,2,0,1,1,1,0,2,1,1,1,1,1,1,2,1,2,1,0,0,2,1,1,1,0,0,0,2,  
0,2,2,1,0,2,1,1,2,2,1,1,1,2,2,2,1,1,1,0,1,0,0]

Expansion in base  $(n/(2^n - 1))$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,0,0,0,0,1,0,0,1,0,1,0,0,0,0,0,0,0,0,0,0,1,0,0,0,0,0,1,1,0,0,0,1,0,0,  
0,1,1,1,1,0,0,1,0,1,0,1,1,1,0,1,0,1,0,0,0,1,0,1,0,0,1,0,0,0,1,1,0,1,1,1,  
,0,  
0,0,0,0,0,0,1,0,1,0,0,0,0,1,0,1,0,0,1,0,1,0,1,1,1,0,1,1,1,1,0,0,0,0,0,0,  
,0,0,0,1,0,1,1,1,1,0,0,0,1,0,0,1,0,0,0,1,1,1,1,0,0,0,0,0,0,0,1,0,1,0,1,  
0,0,0,0,1,1,0,0,1,1,1,1,0,0,0,0,1,0,1,1,1,1,0,1,1,0,0,0,1,0,0,0,0,0,1

Expansion in base  $(n/(2^n + 1))$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,0,0,0,0,1,0,0,1,0,1,0,0,1,0,0,0,0,1,1,0,0,0,1,1,1,0,0,1,0,0,0,  
1,0,1,1,0,1,1,1,0,1,0,0,0,0,1,0,0,0,1,0,0,0,1,1,0,1,1,0,1,0,1,1,0,1,0,1,  
,1,1,0,1,0,1,1,0,0,1,0,1,1,0,0,1,0,0,1,0,1,0,0,1,0,1,1,1,0,0,0,1,1,0,1,  
1,1,1,0,0,1,1,0,0,0,0,1,1,1,0,0,1,1,0,0,1,0,1,0,1,0,1,1,1,1,1,0,1,0,1,0,  
,0,0,0,0,0,0,1,1,1,0,1,0,0,1,1,1,1,0,0,1,0,0,0,1,1,1,0,0,1,0,1,0,0,0,1,  
1,1,0,1,0,1,0,0,0,1,0,1,0,1,0,0,0,0,1,1,0,0,0,1,1,0,1,1,0,0,1,0,1,0,1,1

Expansion in base  $(n/(\exp(n) - 1))$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,0,1,0,0,1,1,1,0,2,0,2,1,0,0,2,0,2,1,0,0,0,1,1,2,0,2,0,2,0,0,2,  
0,0,2,1,1,0,0,1,1,0,1,2,0,1,1,0,0,1,0,2,1,0,0,0,1,2,1,1,2,1,1,0,2,1,1,1,  
,1,0,0,0,2,1,0,1,0,1,2,0,0,2,0,0,2,0,1,0,0,2,0,1,2,0,2,1,1,1,1,1,0,2,  
0,1,0,1,1,0,1,2,0,1,2,0,2,1,2,0,1,0,2,1,1,0,2,0,2,0,0,2,0,2,1,0,2,1,1,1,  
,0,2,0,0,1,1]

Expansion in base  $(n/(\exp(n) + 1))$  of  $1/(1-\text{frac}(x))$  :

[1,0,0,0,0,1,0,0,1,1,2,0,2,1,0,0,0,1,2,0,1,0,0,0,0,0,0,0,1,0,1,0,2,0,0,0,  
2,0,1,0,0,2,0,0,0,2,1,0,2,0,0,1,0,2,1,0,1,1,0,1,1,0,1,2,0,0,0,1,1,0,2,1,  
,1,0,0,0,1,2,1,2,0,0,1,2,1,2,0,0,1,2,0,0,2,1,0,1,0,0,2,1,1,2,0,0,0,2,0,  
0,0,0,2,1,1,0,2,0,1,0,1,0,1,1,2,1,1,0,1,2,1,1,1,0,1,1,0,0,1,2,1,2,0,2,0,  
,2,1,2,0,0,2]

Expansion in base  $(n/(10^n - 1))$  of  $1/(1-\text{frac}(x))$  :

[1,0,1,6,0,2,3,8,0,6,8,6,6,8,3,0,1,3,7,6,6,2,3,7,8,7,4,1,6,1,5,7,3,2,5,  
6,0,9,2,4,6,3,0,0,0,8,0,0,4,9,1,4,7,2,5,2,6,4,0,1,8,1,0,7,4]

Expansion in base  $(n/(10^n + 1))$  of  $1/(1-\text{frac}(x))$  :

[1,0,1,6,1,3,1,5,3,0,5,2,6,9,0,2,0,3,2,3,2,6,2,0,0,4,1,3,7,3,7,5,2,4,2,  
2,7,5,3,8,4,1,1,6,8,1,2,3,3,6,5,7,3,8,5,7,8,6,7,9,7,5,7,7,3]

Appendix

Dessin de  $\pi$  Yves Chiricota, 1995



$\pi$   
Y.C.

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